

# First-principles study of phosphors for white-LED applications

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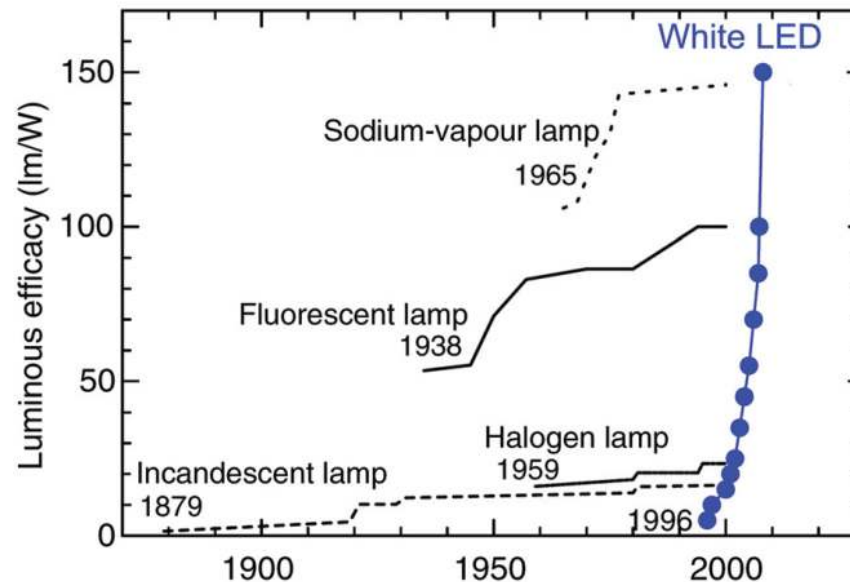
 UCLouvain

 Skoltech  RSF  Russian Science Foundation

Moscow, November 11, 2020

# Lighting : energy consumption ...

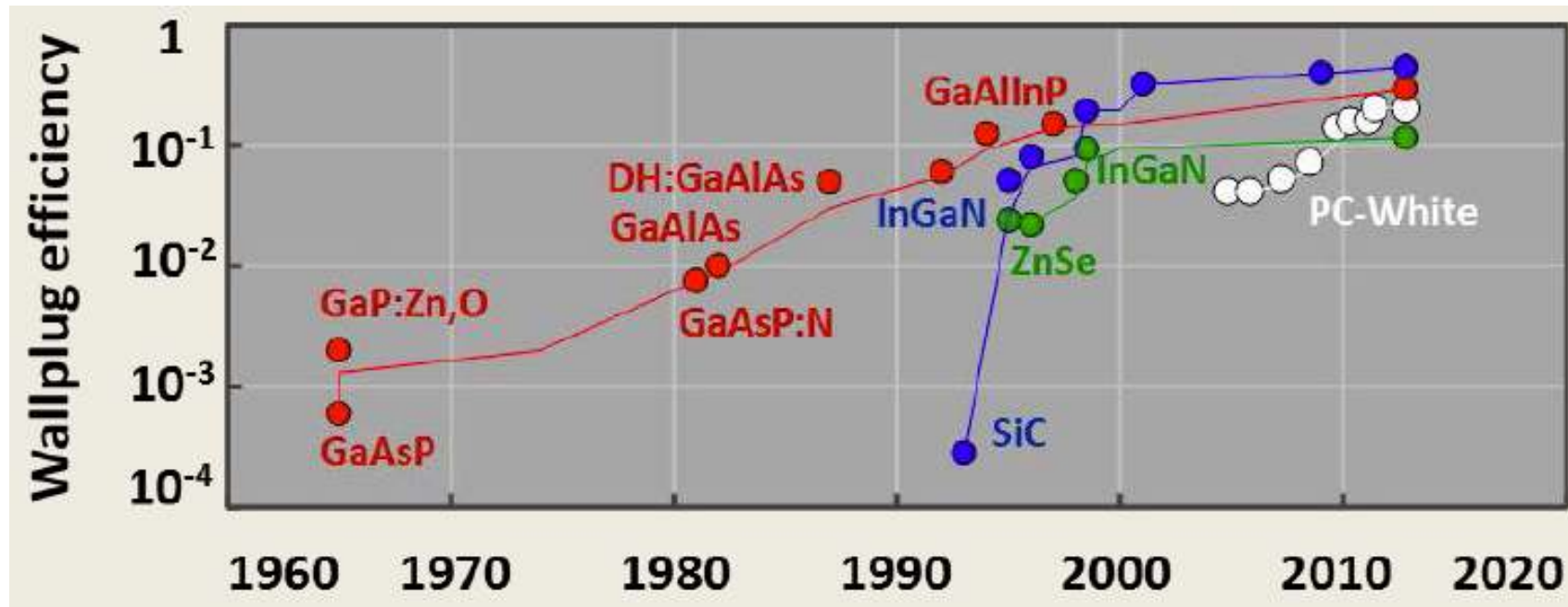
“Lighting represents almost **20% of global electricity consumption**. This consumption is similar to the amount of electricity generated by nuclear power.” (*Int. Energy Agency*)



lm = Lumen = SI unit for the total *visible* flux emitted by a source  
Includes luminosity function ; 1 W of green light (555 nm) => 683 lm

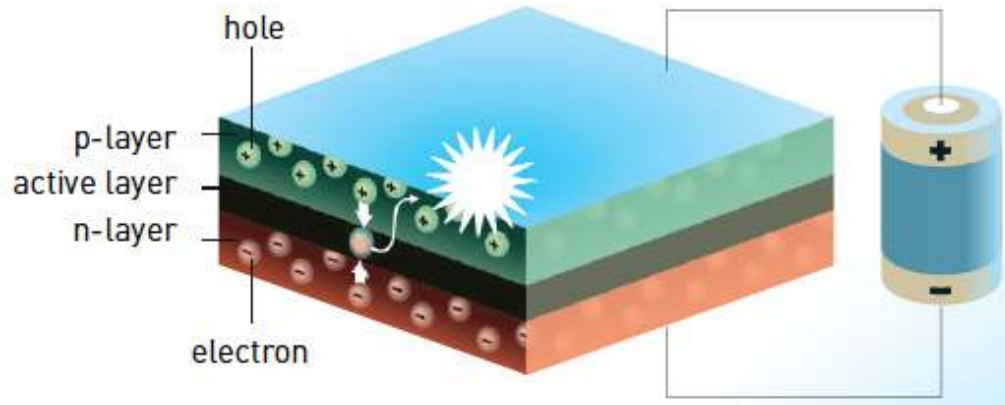
# Efficiency of light-emitting diodes : decades of improvements

Red ... blue ... Nobel prize in physics 2014 Akasaki, Amano, Nakamura + phosphor => PC-White : Phosphor converted white-light

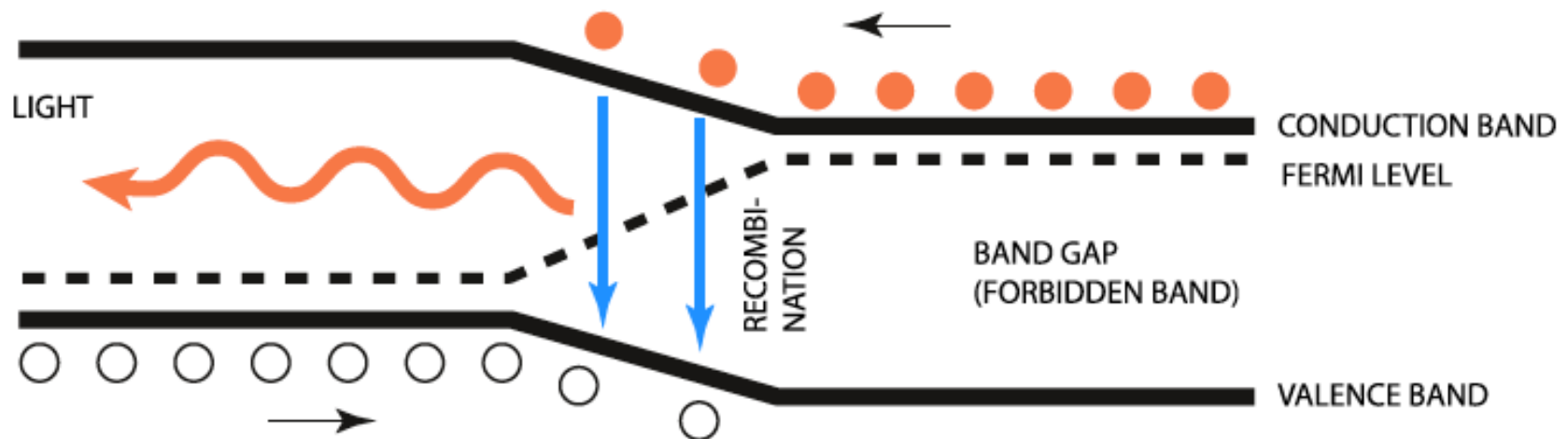


Wall plug efficiency : ratio between electrical power (in) and optical power (out)

# Electroluminescence : Light-emitting diode

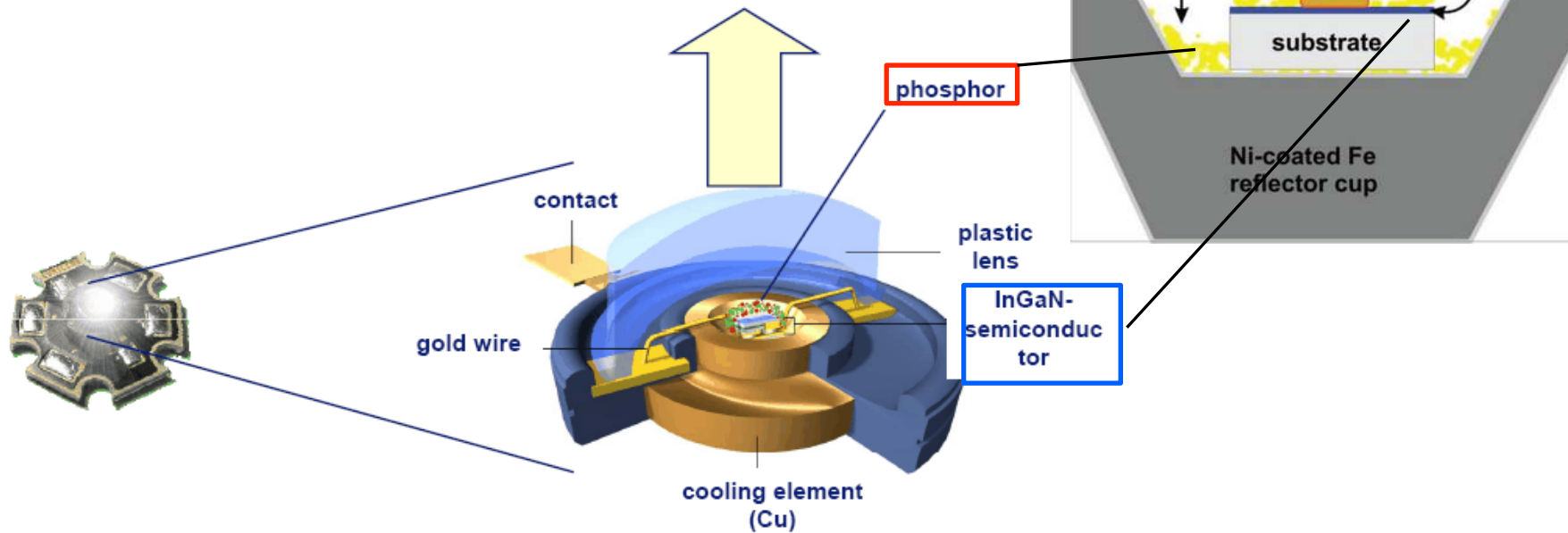


Applying an adequate difference of potential inject holes in the p-region and electrons in the n-region => electron-hole pairs



# Standard white PC-LED

The most efficient white LEDs are phosphor-based :  
downconversion of blue light



**(In, Ga)N semiconductor chip + phosphors**

**White light**

**Blue chip, 420-480 nm**

**yellow phosphor**

**cool white**

**Blue chip, 420-480 nm**

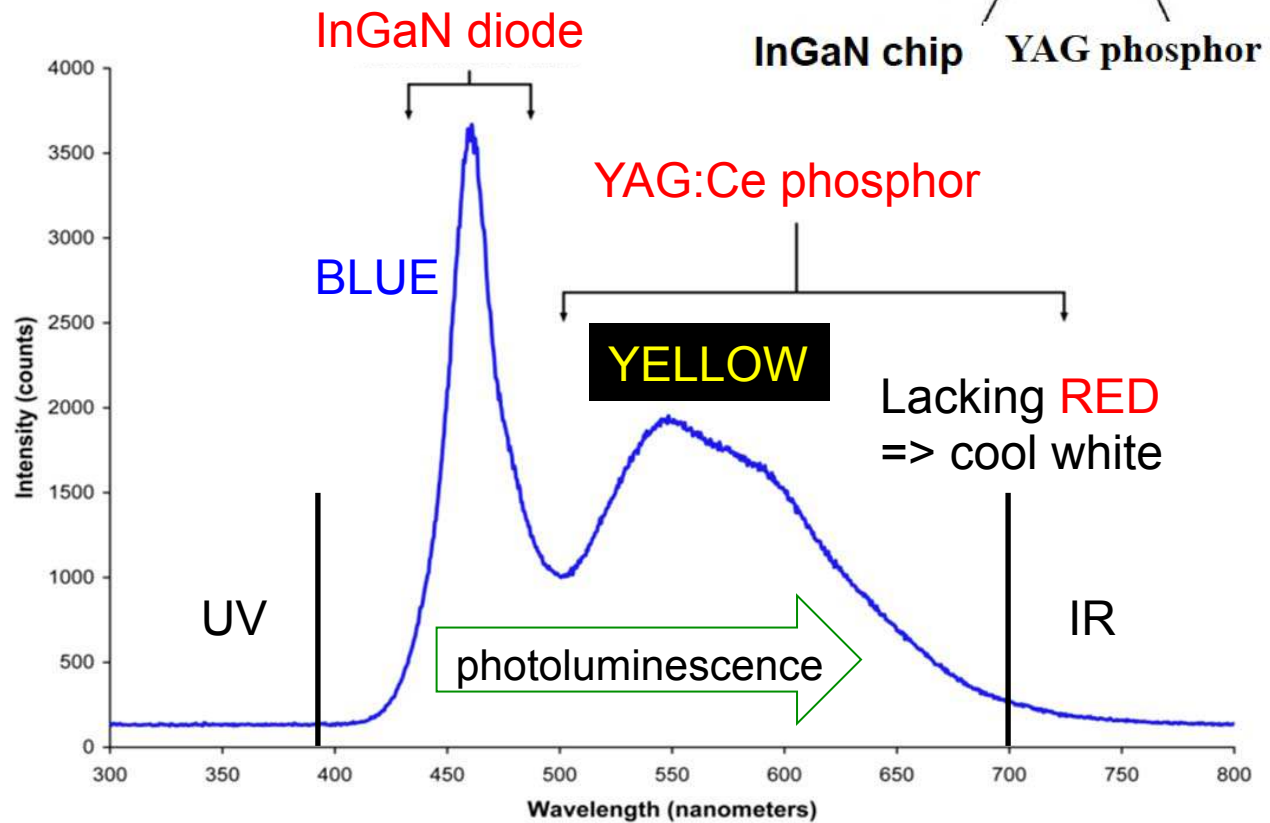
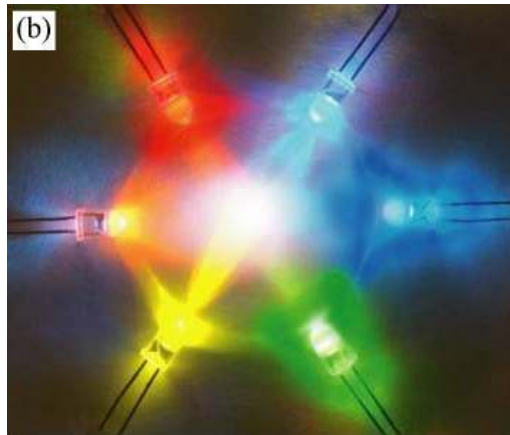
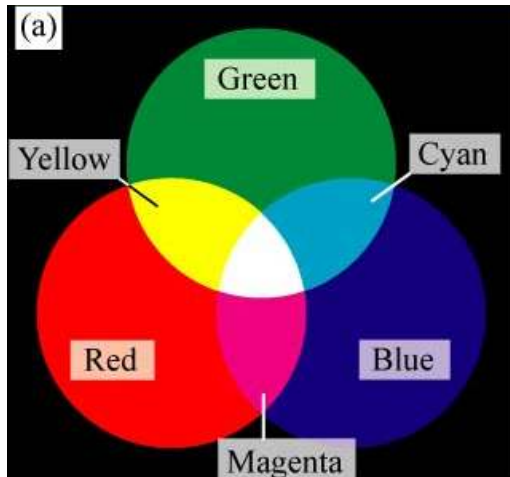
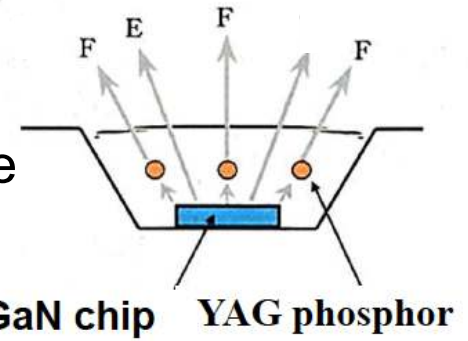
**R+G phosphor blends**

**warm white**

# Blue+yellow LED emission spectrum

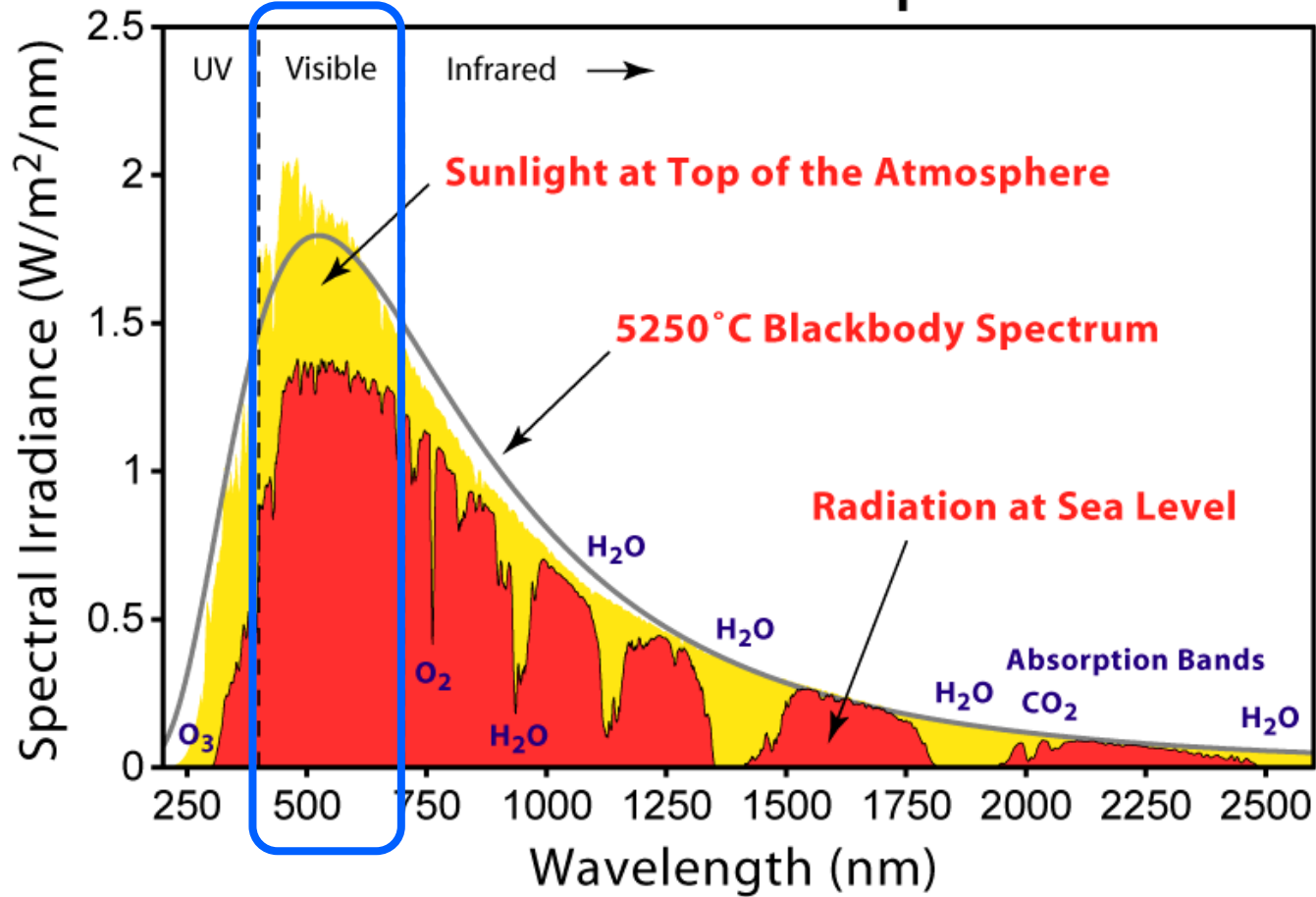
Downconversion of blue light

by Yttrium Aluminum Garnet : Ce



# Compare with solar spectrum

## Solar Radiation Spectrum



# Wide diversity of LED+phosphors

Conventional type

Blue-LED + yellow phosphor  
(typically,  $Y_3Al_5O_{12}:Ce^{3+}$ )

High color rendering types

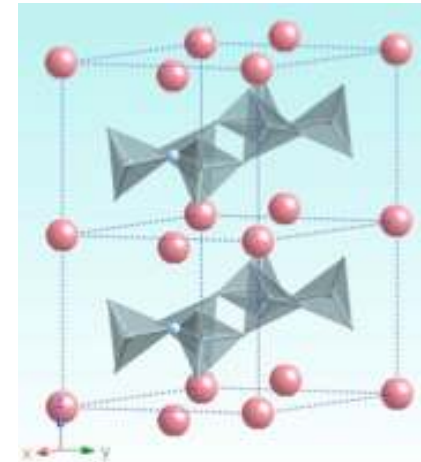
Blue-LED + yellow & red

Near UV-LED + blue & green & red

Blue-LED + green & red

Tab. 1.3 Spectral position of the emission band of  $Eu^{2+}$  in some representative lattices.

$SrB_4O_7:Eu$	368 nm
$Sr_2P_2O_7:Eu$	420 nm
$BaMgAl_{10}O_{17}:Eu$	453 nm
$Sr_4Al_{14}O_{25}:Eu$	490 nm
$Ba_2SiO_4:Eu$	505 nm
$SrGa_2S_4:Eu$	535 nm
$Sr_2SiO_4:Eu$	575 nm
$SrS:Eu$	615 nm



Phosphor tuning ? Host/dopant ? Selection criterion ?



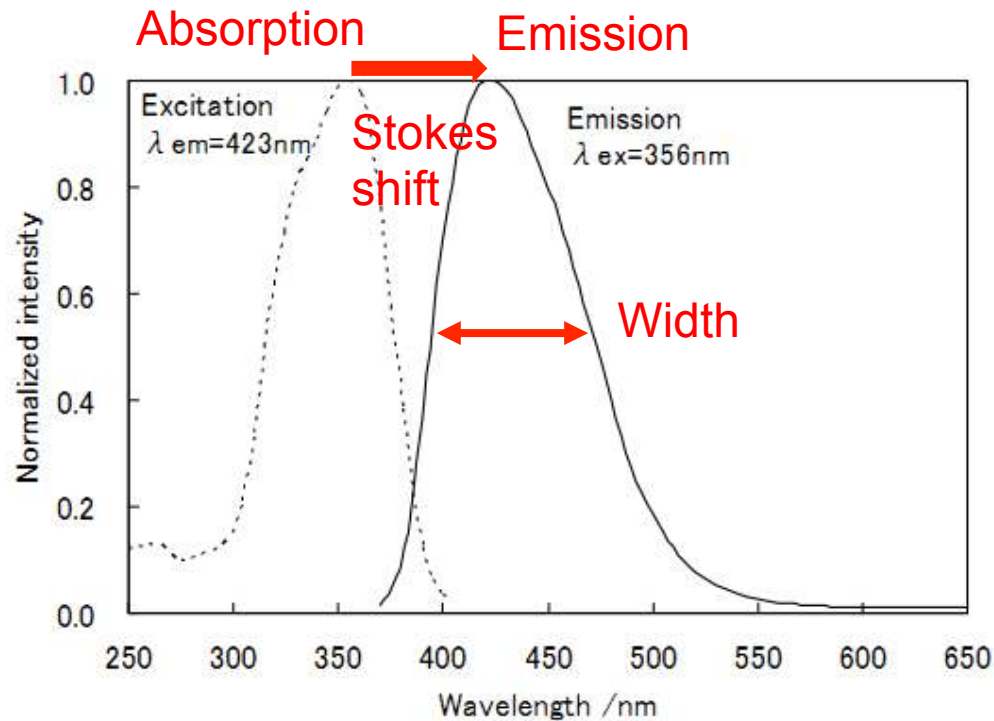
# Overview

1. Role of phosphors in white-LEDs
2. Working principles, selection criteria, 4f-5d phosphors
3. How to model ? First-principles ... but not too much !
4. Theoretical study of lanthanum silicon nitrides hosts + Ce
5. Scaling up : results for 28 different hosts
6. Thermal quenching, width of emission, beyond 1D model

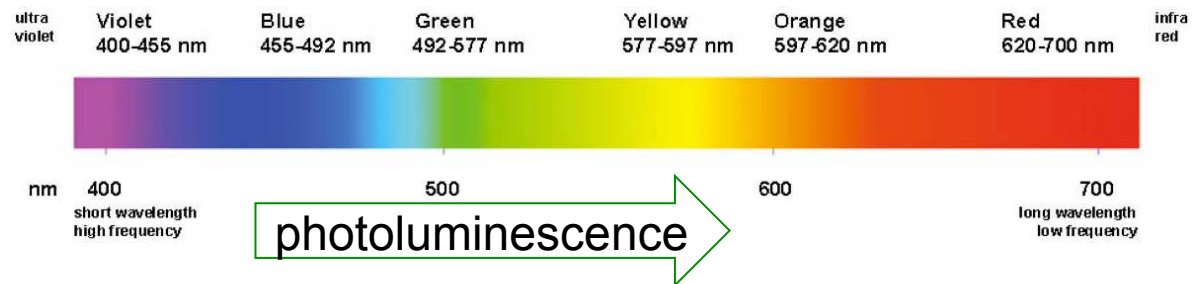
## References :

- Y. Jia, A. Miglio, S. Poncé, X. Gonze and M. Mikami, *Phys. Rev. B* **93** 155111 (2016)  
X. Gonze *et al*, *Comput. Phys. Commun.* **205**, 106 (2016)  
Y. Jia, A. Miglio, S. Poncé, M. Mikami and X. Gonze, *Adv. Opt. Materials*, **5**, 1600997 (2017)  
Y. Jia, A. Miglio, S. Poncé, M. Mikami and X. Gonze, *Phys. Rev. B* **96**, 125132 (2017)  
Y. Jia, A. Miglio, M. Mikami and X. Gonze, *Phys. Rev. Mat.* **2**, 125202 (2018)  
Y. Jia, A. Miglio, S. Poncé, M. Mikami and X. Gonze, *Phys. Rev. B* **100**, 155109 (2019)  
J. Bouquiaux, Y. Jia, S. Poncé, A. Miglio, M. Mikami & X. Gonze, *arXiv:cond-mat.mtrl-sci 2010:00423* (2020)  
+ Review on phosphors :  
P. F. Smets, A. B. Parmentier and D. Poelmans  
“Selecting Conversion Phosphors for White Light-Emitting Diodes”  
*J. Electrochemical Society* **158** R37 (2011)

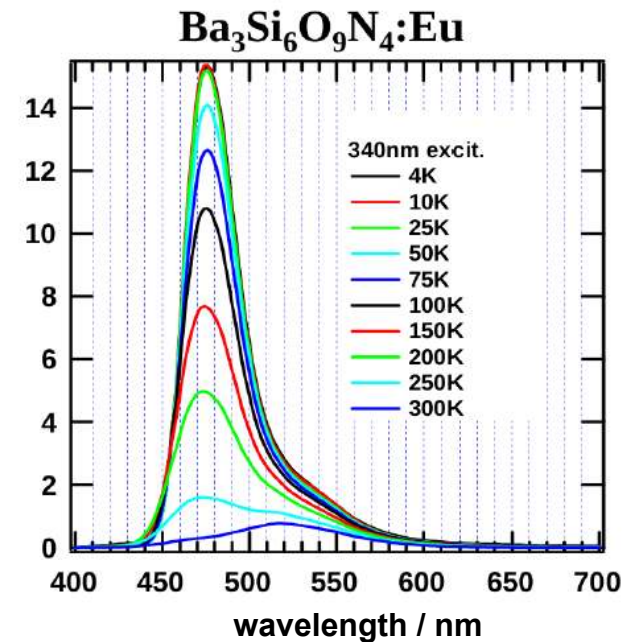
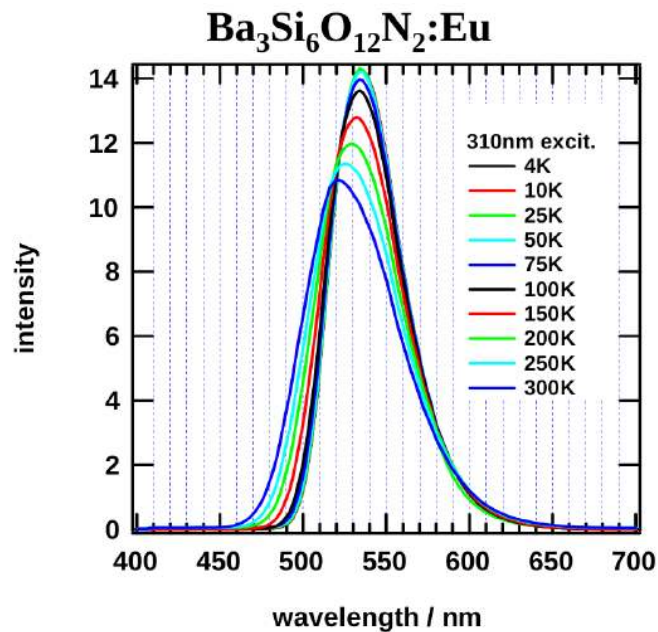
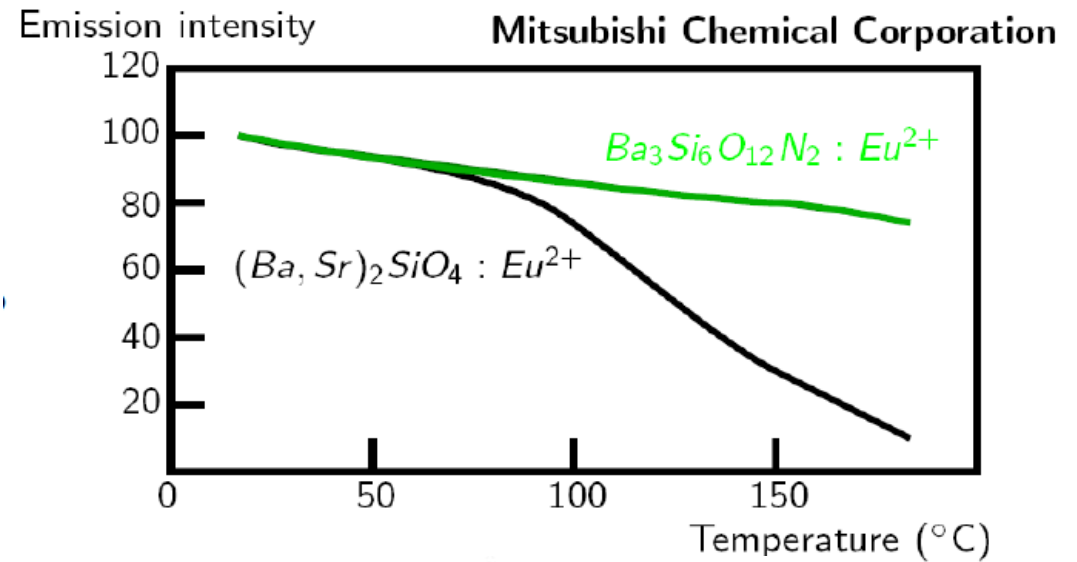
# Absorption/emission/Stokes shift



- (1) Absorption occurs
- (2) Atomic configuration changes, decreasing the energy
- (3) Emission occurs



# Thermal quenching



See e.g. C. Braun ... W. Schnick, Chem. Eur. J. 16, 9646 (2010)

# Criteria for selecting phosphors

1. **Emission spectrum** that complements adequately the LED (+ other phosphors if use more than one)  
Importance of **linewidth** (missing: good red narrow width phosphor)
2. **Excitation spectrum** with good overlap with the pumping LED, and large absorption strength
3. **Optical characteristics** unchanged at **elevated temperature (450K)**
4. **Quantum efficiency** approaching unity
5. Chemical **stability**
6. Absence of emission saturation at **high fluxes**

# Ce- and Eu- doped inorganic hosts

Best choice (at present) :

**Ce<sup>3+</sup> and Eu<sup>2+</sup> - doped « inorganic hosts » : 4f – 5d transition**

[ternary/quaternary silicates, phosphates, (oxy)nitrides, (oxy)sulfides, etc]

Ce and Eu substitutional to trivalent or divalent ions

Large absorption strength

Excellent quantum efficiency (>90% for YAG:Ce)

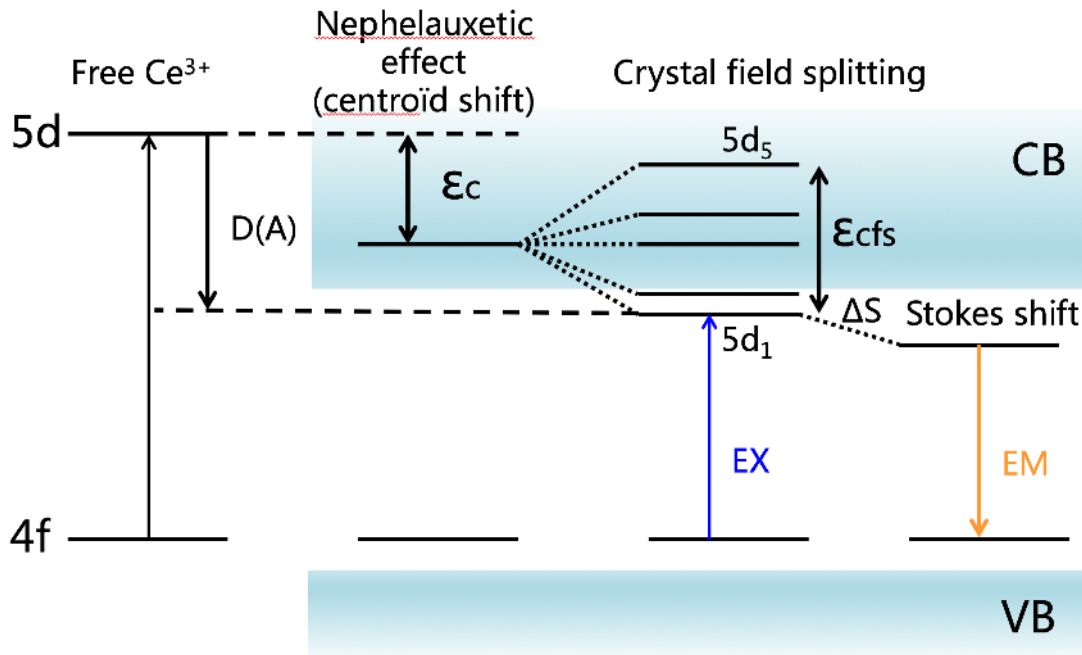
Tunable

**But : Thermal quenching ? Adequate emission band ?**

How can theory help for such complex materials ?

High-throughput search, but which indicators ?

# Dorenbos model for 4f – 5d transition



$$D(A) = \epsilon_c(A) + \frac{\epsilon_{cfs}(A)}{r(A)} - 1890cm^{-1}$$

$$\epsilon_c(A) = 1.44 \times 10^{17} \sum_{i=1}^N \frac{\alpha_{sp}^i}{R_i^6}$$

$$\alpha_{sp} = \alpha_0 + \frac{b}{\chi^2}$$

$$\epsilon_{cfs} = \frac{\beta}{R_{av}^2}$$

Depend on type of coordination incl. # NN

$$E(A) = 49340cm^{-1} - D(A)$$

4f – 4f transitions :

- do not show as nice a tunability
- narrow absorption range => colour drift with T

Dorenbos, PRB, 62, 15640 (2000)  
 Dorenbos, PRB, 62, 15650 (2000)  
 Dorenbos, PRB, 64, 125117 (2001)  
 Dorenbos, PRB, 65, 235110 (2002)  
 Liu et al, J. Lumin, 166, 106 (2016)

# How to model ? First-principles ... but not too much !

# Search for better phosphors

- Empirical or semi-empirical search (cf Dorenbos)
  - exp. data (e.g. emission) for >100 doped hosts
  - ? quality of material
  - ? data for linewidth, thermal quenching
- Machine-learning based on such exp. data ?
- First-principles :
  - either give new data for machine-learning (need accuracy)
  - or allow direct high-throughput search (need speed)



# Challenge for first-principles

- Optical excitations => electron-hole interaction !
- Bethe-Salpeter equation (BSE) ?!
- Supercells - 60 ... 120 atoms (Eu, Ce 6.25% - 12.5%)
- Ce, Eu => 4f electrons !
- “Big” cells : cannot afford BSE
- Need to relax the geometry !
- Simpler approaches to generate indicators ?

Ground state only ? Doped ? Bulk undoped ?

... And how address linewidth ?

... Thermal quenching ?

# Indicators : speed vs accuracy



Accuracy



Bethe-Salpeter Equation  
(+ geometry relaxation)

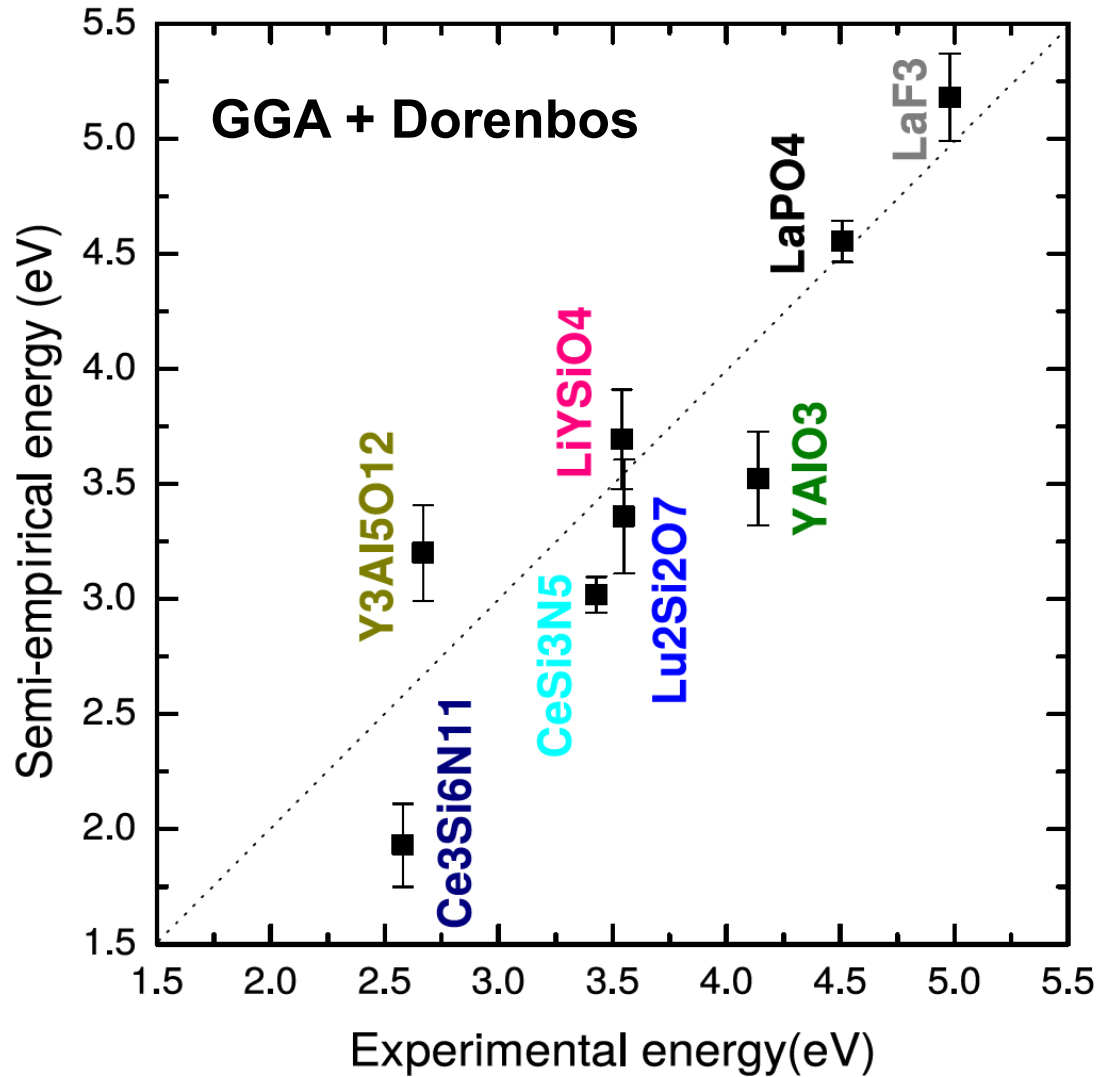
Doped ground-state + Dorenbos model

Undoped bulk



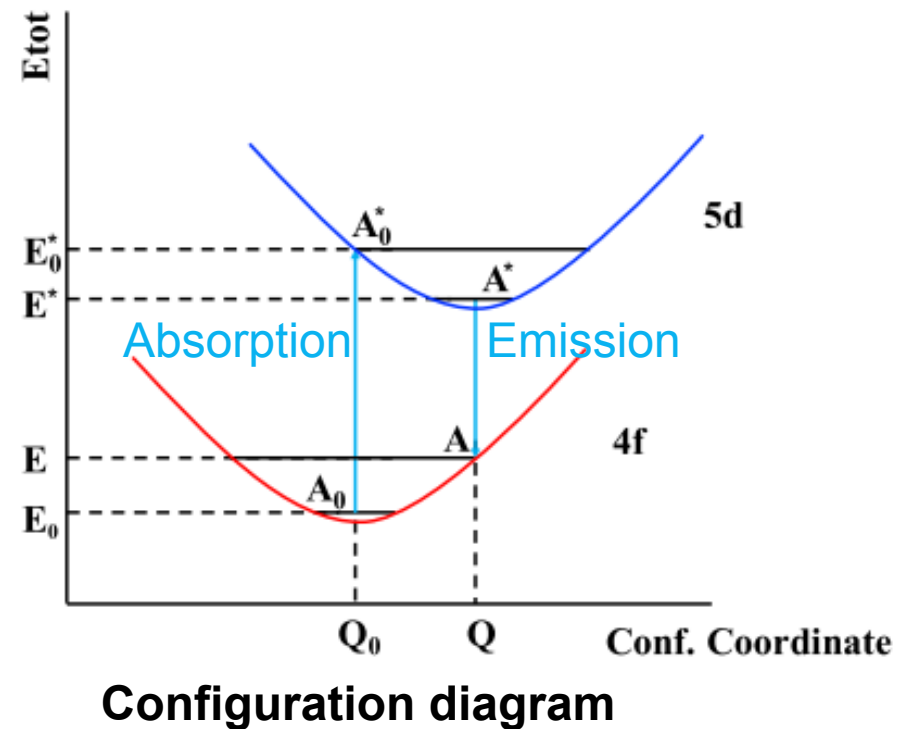
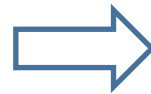
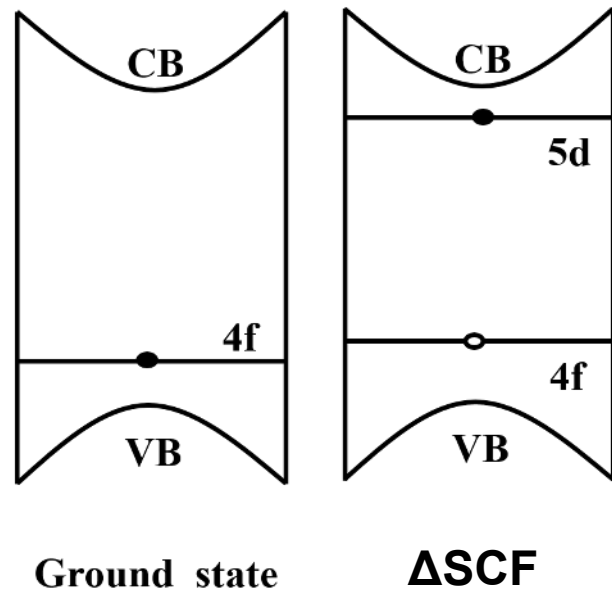
Speed

# Absorption: GGA + Dorenbos model



Still :  
How to predict  
emission ?  
What is the excited  
state geometry ?

# $\Delta$ SCF method



- $\Delta$ SCF method: mimic **the interaction between electrons and a 4f-hole**. Comparison of total energies of ground and excited states.
- Calculate transition energy based on configuration coordination diagram  
(Seitz 1938, Mott 1938, Gurney 1939 ...).

For scintillator absorption see also : Chaudhry, Canning et al, PRB 83, 125155 (2011), JAP 109, 083708 (2011), PRB 89, 155105 (2014)

# Indicators : speed vs accuracy



Accuracy



Bethe-Salpeter Equation  
(+ geometry relaxation)

$\Delta$ SCF with 1D configuration diagram

Doped ground-state + Dorenbos model

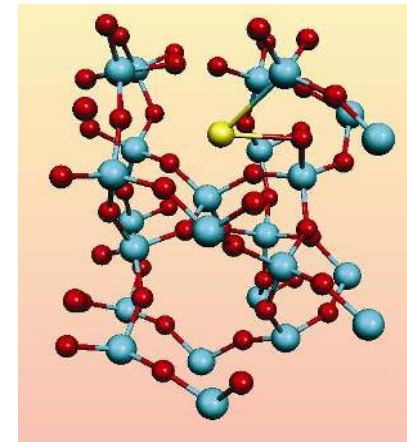
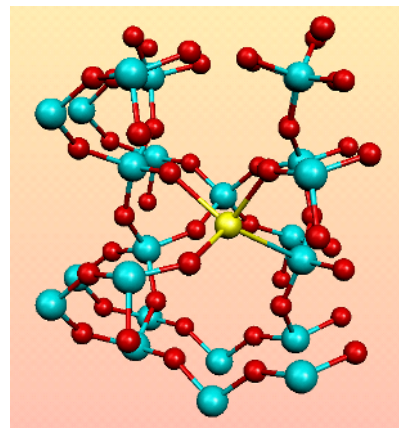
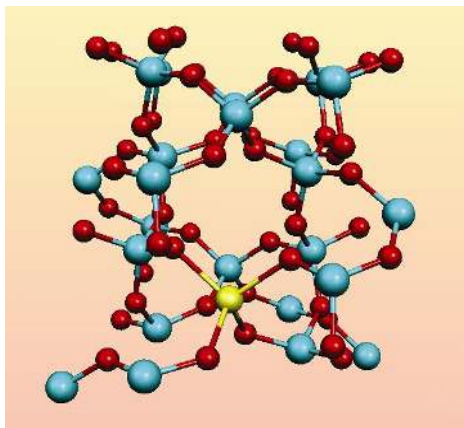
Undoped bulk



Speed

# First-principles calculations

- Density functional theory (DFT) +U => **Total energy + bands**
- Abinit software (<http://www.abinit.org>)
- Projector Augmented Wave (PAW) + Plane Waves
- Cutoff energy: 30Ha
- Supercells - 60 ... 120 atoms (Eu, Ce 6.25% - 12.5%)



# ABINIT software project

Implementing Density-Functional Theory + Many-body Perturbation Theory.  
For solids and nanosystems, computation of :  
energetics, electronic structure, vibrations, dielectric responses,  
optic, Raman, thermodynamics, ...

## 1997 Ideas :

- 1) Target a wide range of capabilities => need a worldwide collaboration
- 2) Linux software development : 'free software' model

## 1997... 2019 Development :

Releases of ABINIT (v1.0.0 to v8.10.2)  
8 international ABINIT developer  
workshops (40 ... 60 participants)

## 2019 Assessment :

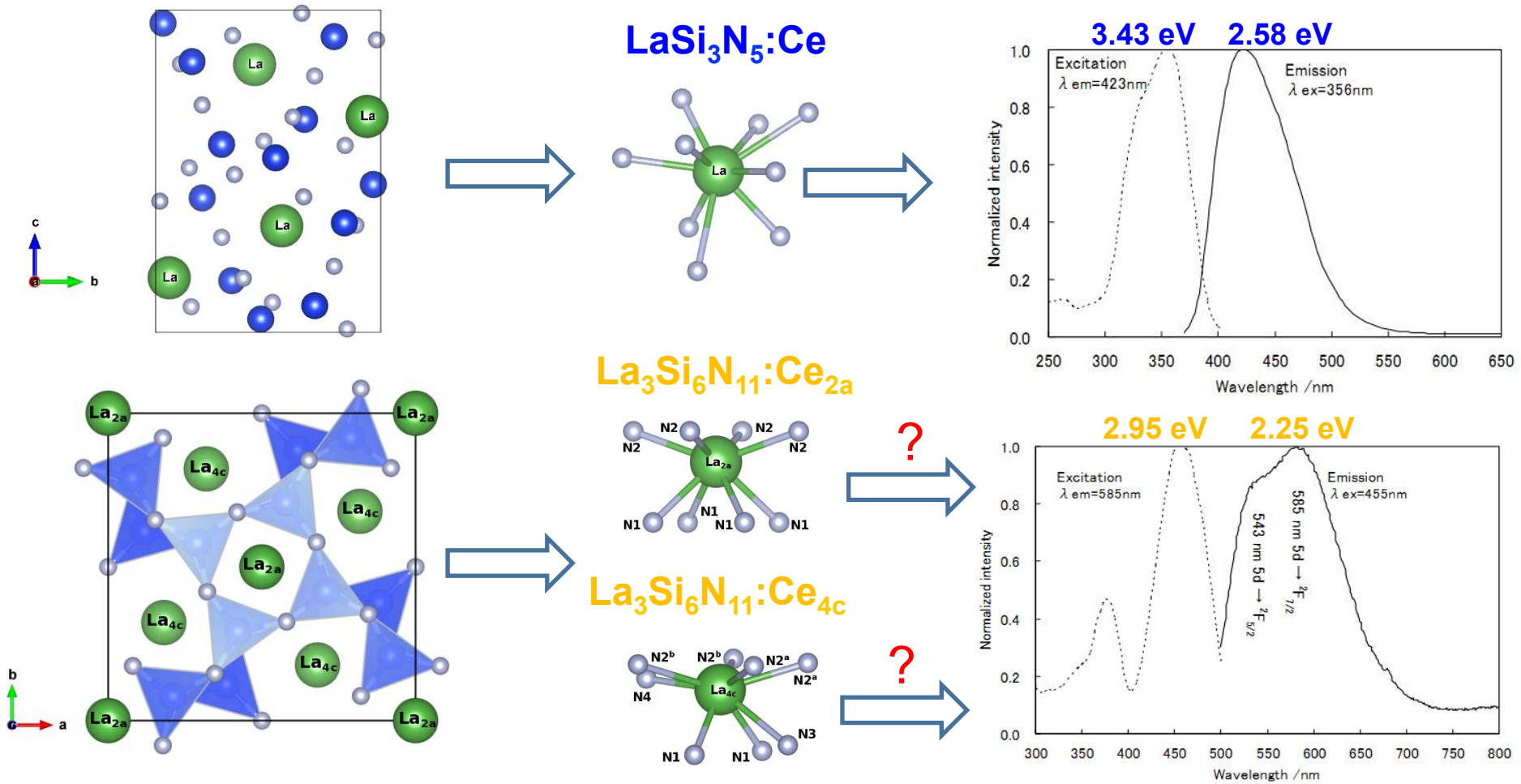
>2000 members on the forum  
800 kLines of F90  
about 50 contributors to ABINITv8



# Ab Initio at work: Ce-doped lanthanum silicon nitrides



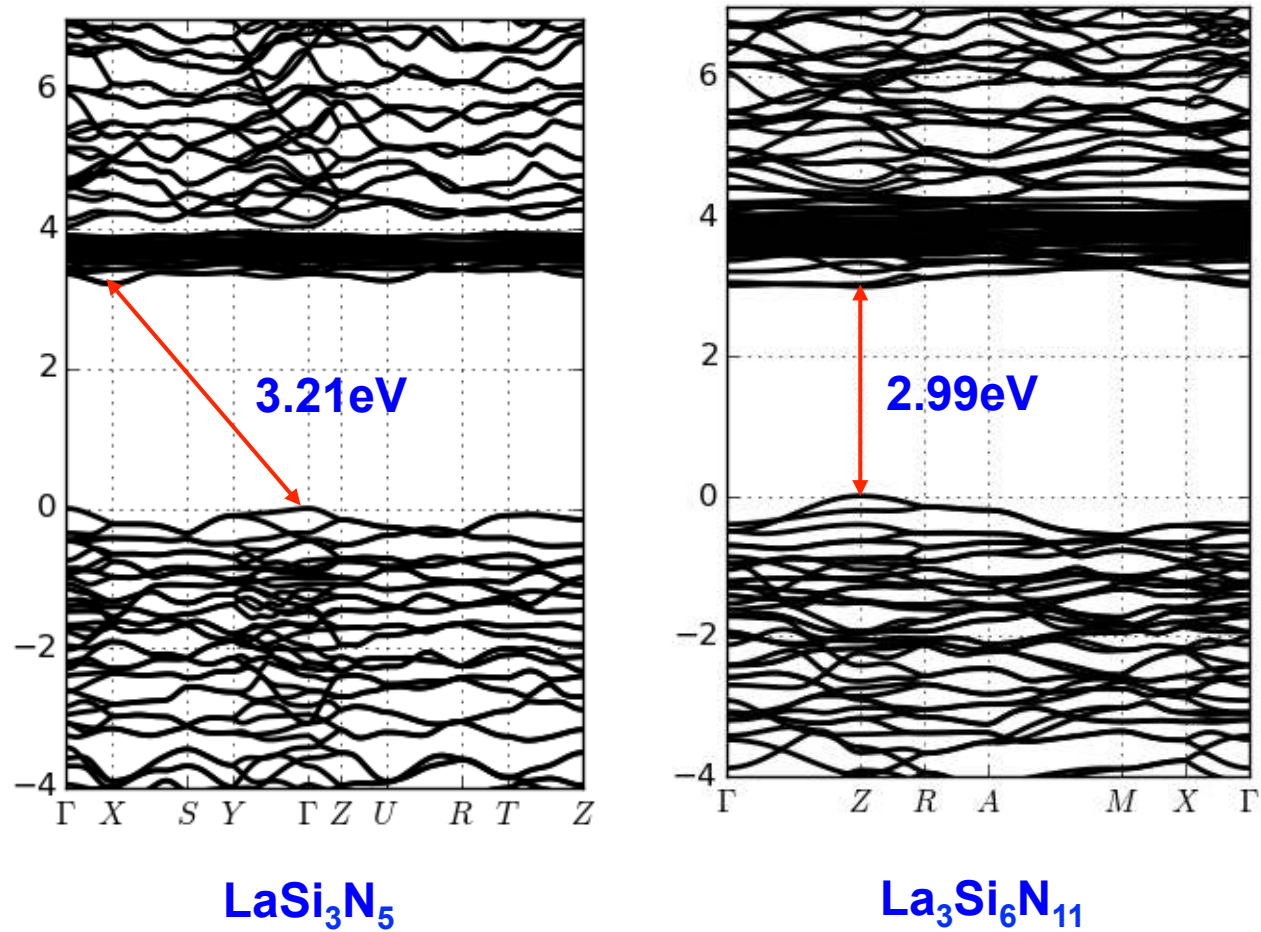
# Ce<sup>3+</sup> ion in LaSi<sub>3</sub>N<sub>5</sub> and La<sub>3</sub>Si<sub>6</sub>N<sub>11</sub> (LSN)



- The reason for the different emission color ?
- The luminescent center in the La<sub>3</sub>Si<sub>6</sub>N<sub>11</sub>:Ce ?

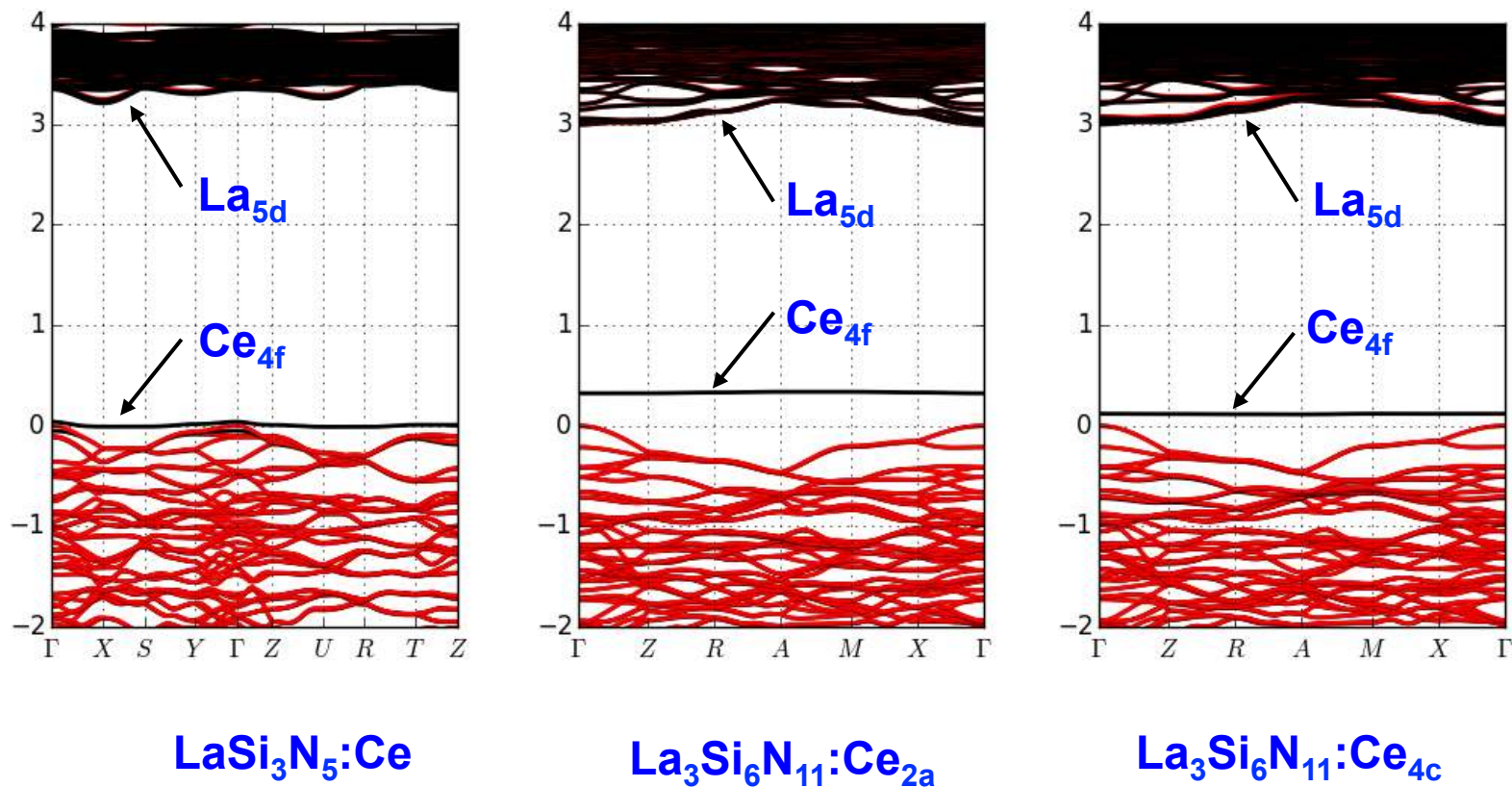
Suehiro et al, APL, 95, 051903(2009)  
Kijma et al, ECS Trans. 25, 247 (2009)

# LSN DFT electronic structure



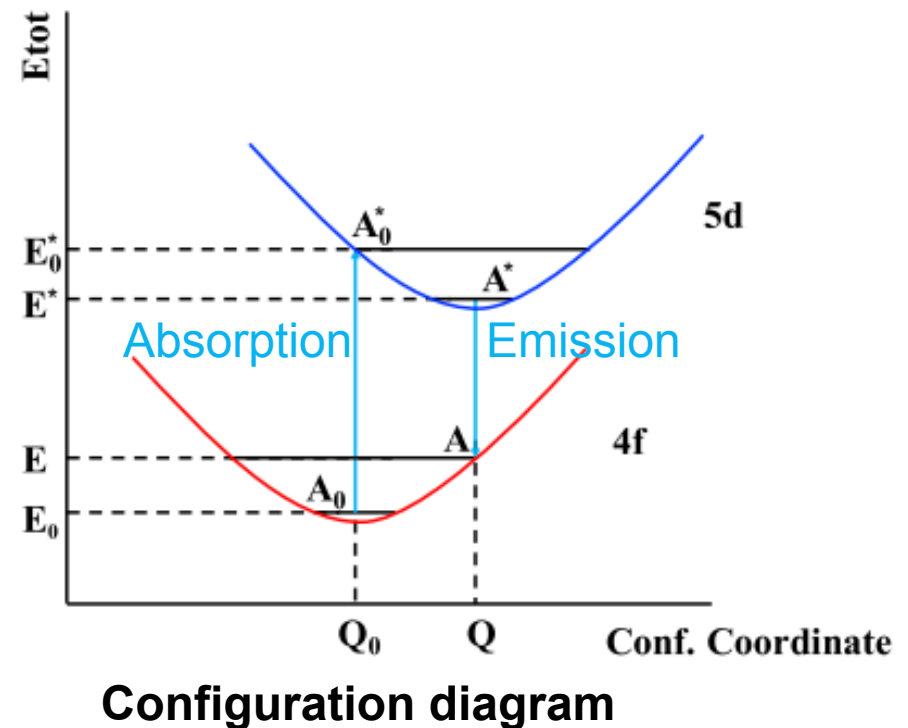
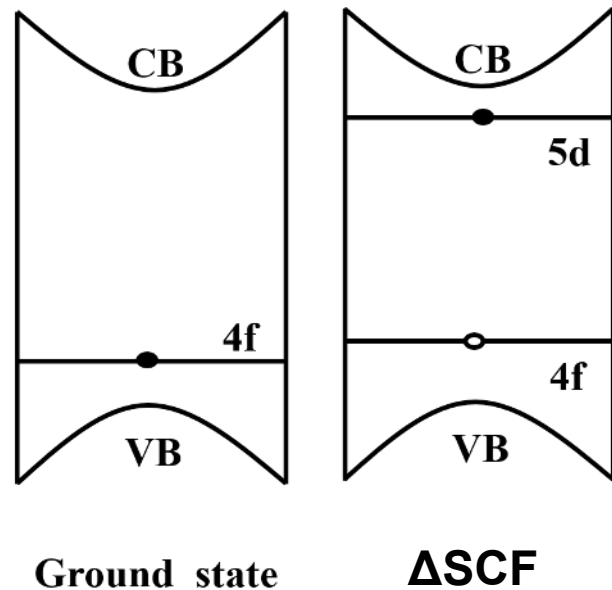
■ Ab-initio simulation: Density functional theory (DFT), GGA level

# Ce-doped LSN : DFT electronic structure



- The description of  $Ce_{4f}$  state relies on the DFT+U method,  $U = 4.6eV$
- $Ce_{5d}$  state not located inside band gap in ground state calculation  
(DOES **NOT** correspond to luminescent excited state of LSN:Ce)

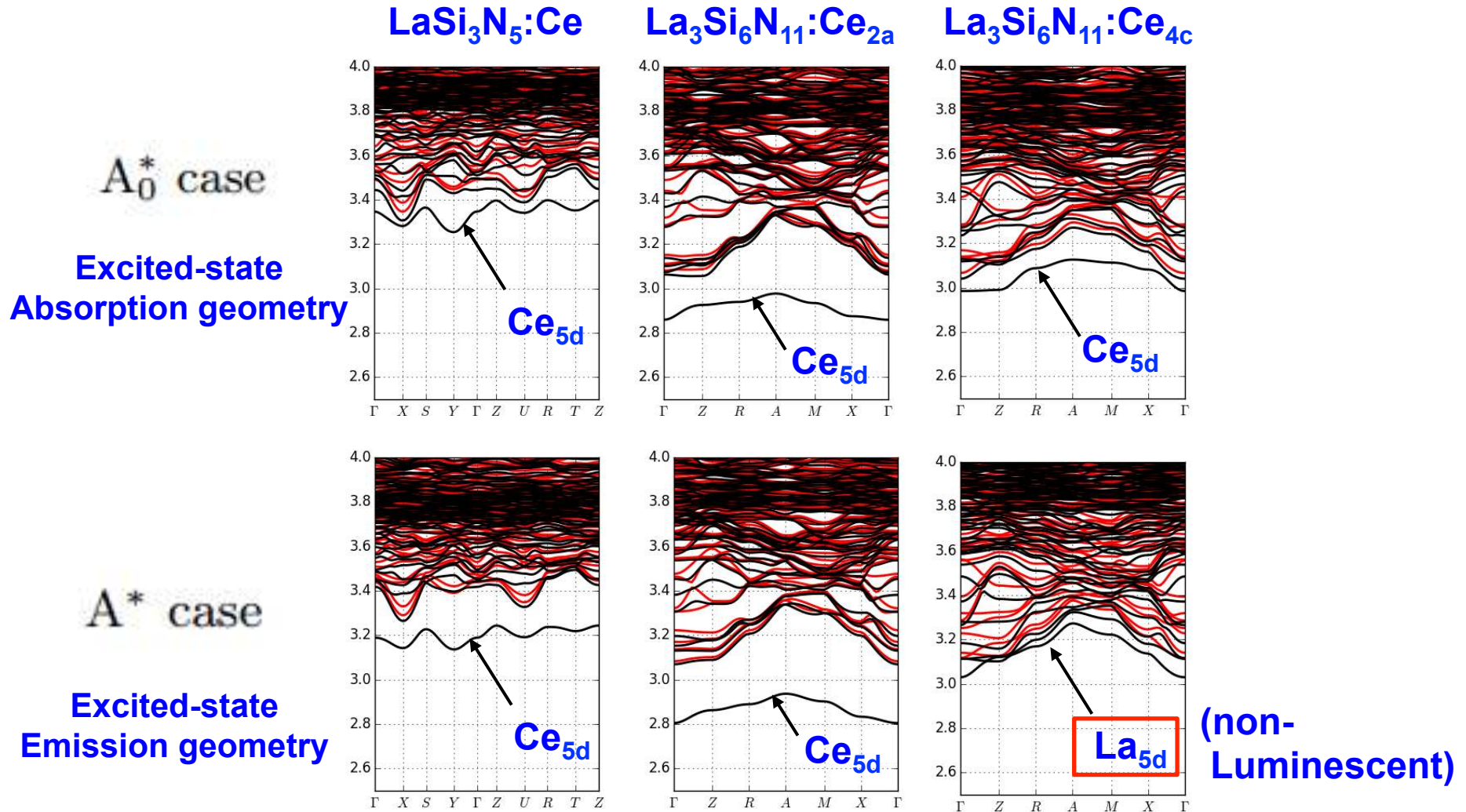
# $\Delta$ SCF method



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For scintillator absorption see also : Chaudhry, Canning et al, PRB 83, 125155 (2011), JAP 109, 083708 (2011), PRB 89, 155105 (2014)

# Ce-doped LSN : excited state electronic structure



- Core-hole interaction and anti-bonding character affect position of Ce<sub>5d</sub> state

# $\Delta$ SCF Energies in ground- and excited-states

Case	LaSi <sub>3</sub> N <sub>5</sub> :Ce	La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>2a</sub>	La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>4c</sub>
A <sub>0</sub>	-20774.76eV	-25363.89eV	-25363.98eV
A <sub>0</sub> *	-20771.26eV	-25361.10eV	-25360.70eV
A	-20774.53eV	-25363.68eV	-25363.52eV
A*	-20771.42eV	-25361.28eV	-25360.92eV
$\Delta E_{\text{abs}}(A_0^*-A_0)$	3.50eV	2.79eV	3.28eV
$\Delta E_{\text{abs}}(\text{Exp.})$	3.43eV	2.58eV	-----
$\Delta E_{\text{em}}(A^*-A)$	3.12eV	2.40eV	2.60eV
$\Delta E_{\text{em}}(\text{Exp.})$	2.95eV	2.25eV	-----
$\Delta S(\text{Cal.})$	3080cm <sup>-1</sup>	3160cm <sup>-1</sup>	5456cm <sup>-1</sup>
$\Delta S(\text{Exp.})$	3815cm <sup>-1</sup>	2717cm <sup>-1</sup>	-----

$1000\text{cm}^{-1}=0.124\text{eV}$  Y. Jia *et al*, PRB, 93, 15111 (2016)

- Accurate absorption and emission energy, within 0.2eV error.
- Stokes shift value is provided within 20% difference.
- Luminescent center in La<sub>3</sub>Si<sub>6</sub>N<sub>11</sub>:Ce is determined to be Ce<sub>2a</sub> site



# Ce environment and Dorenbos model parameters

LaSi <sub>3</sub> N <sub>5</sub> :Ce			9 NN
Bond	Ground	Excited	Geometry
Ce-N1 <sup>a</sup>	3.151	3.178	
Ce-N1 <sup>b</sup>	3.137	<b>3.324</b>	
Ce-N2 <sup>a</sup>	2.430	2.380	
Ce-N2 <sup>b</sup>	2.717	<b>2.601</b>	
Ce-N3	2.874	2.955	
Ce-N4 <sup>a</sup>	2.553	2.416	
Ce-N4 <sup>b</sup>	2.898	2.835	
Ce-N5 <sup>a</sup>	2.690	2.792	
Ce-N5 <sup>b</sup>	2.850	<b>2.712</b>	

La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>2a</sub>			8 NN
Bond	Ground	Excited	Geometry
Ce-N1 (x4)	2.657	2.645	
Ce-N2 (x4)	2.638	<b>2.555</b>	

La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>4c</sub>			8 NN
Bond	Ground	Excited	Geometry
Ce-N1(x2)	2.512	2.389	
Ce-N2 <sup>a</sup> (x2)	2.670	2.596	
Ce-N2 <sup>b</sup> (x2)	2.901	2.895	
Ce-N3	2.802	2.718	
Ce-N4	2.641	<b>2.472</b>	

	LaSi <sub>3</sub> N <sub>5</sub> :Ce	La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>2a</sub>	La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce <sub>4c</sub>
$\chi_{av}$	1.74	1.68	1.68
$\alpha_{sp}^N$	7.07	7.52	7.52
$\epsilon_c$ , GS	21380 cm <sup>-1</sup>	25166 cm <sup>-1</sup>	23671 cm <sup>-1</sup>
$\epsilon_c$ , EX	23950 cm <sup>-1</sup>	28242 cm <sup>-1</sup>	–
$\beta$	$5.67 \times 10^8$	$1.20 \times 10^9$	$1.20 \times 10^9$
$R_{av}$ , GS	281 pm	265 pm	270 pm
$R_{av}$ , EX	280 pm	260 pm	–
$\epsilon_{cfs}$ , GS	7181 cm <sup>-1</sup>	17088 cm <sup>-1</sup>	16461 cm <sup>-1</sup>
$\epsilon_{cfs}$ , EX	7232 cm <sup>-1</sup>	17751 cm <sup>-1</sup>	–

$$D(A) = \epsilon_c(A) + \frac{\epsilon_{cfs}(A)}{r(A)} - 1890cm^{-1}$$

$$\epsilon_c(A) = 1.44 \times 10^{17} \sum_{i=1}^N \frac{\alpha_{sp}^i}{R_i^6}$$

$$\alpha_{sp} = \alpha_0 + \frac{b}{\chi^2}$$

$$\epsilon_{cfs} = \frac{\beta}{R_{av}^2}$$

Depend on type of coordination incl. # NN

$$E(A) = 49340cm^{-1} - D(A)$$

# Scaling up : results for 28 Ce- and Eu- doped hosts



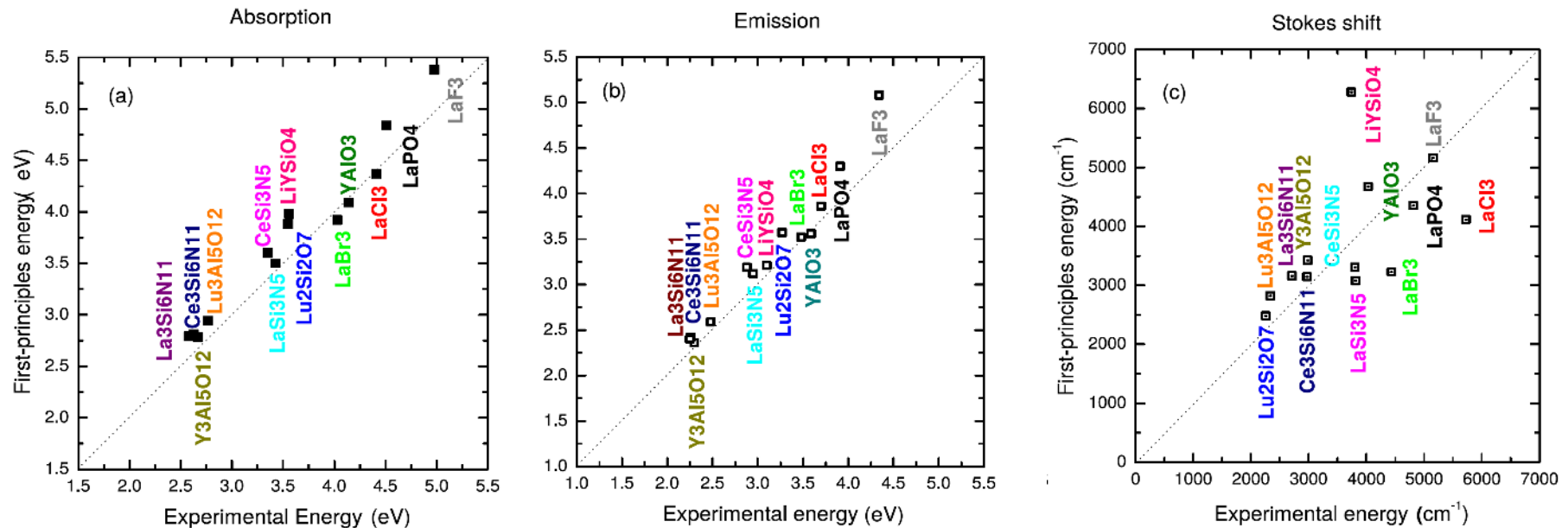
# Thirteen Ce-doped hosts covering 2-5 eV range

Compounds	Calculation (this work)			Experiment		
	Abs (eV)	Em (eV)	$\Delta S$ (cm <sup>-1</sup> )	Abs (eV)	Em (eV)	$\Delta S$ (cm <sup>-1</sup> )
<b>LSN</b> → La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce	2.79	2.40	3160	2.58	2.25	2710
Ce <sub>3</sub> Si <sub>6</sub> N <sub>11</sub>	2.81	2.42	3146	2.63	2.26	2974
<b>YAG</b> → Y <sub>3</sub> Al <sub>5</sub> O <sub>12</sub> :Ce	2.78	2.36	3424	2.67	2.30	2984
Lu <sub>3</sub> Al <sub>5</sub> O <sub>12</sub> :Ce	2.94	2.59	2823	2.77	2.48	2339
CeSi <sub>3</sub> N <sub>5</sub>	3.60	3.19	3307	3.35	2.88	3815
<b>LSN</b> → LaSi <sub>3</sub> N <sub>5</sub> :Ce	3.50	3.12	3080	3.43	2.95	3815
LiYSiO <sub>4</sub> :Ce	4.02	3.33	5575	3.54	3.10	3740
Lu <sub>2</sub> Si <sub>2</sub> O <sub>7</sub> :Ce	3.88	3.57	2480	3.55	3.27	2258
LaBr <sub>3</sub> :Ce	3.92	3.52	3226	4.03	3.48	4439
YAlO <sub>3</sub> :Ce	4.14	3.56	4678	4.09	3.59	4033
LaCl <sub>3</sub> :Ce	4.37	3.86	4113	4.41	3.70	5726
LaPO <sub>4</sub> :Ce	4.84	4.30	4355	4.51	3.91	4818
LaF <sub>3</sub> :Ce	5.38	4.74	5162	4.98	4.34	5162

Jia, Poncé, Miglio, Mikami & Gonze, *Adv. Opt. Materials*, 5, 1600997(2017)

# Wide applicability of the first-principles methodology

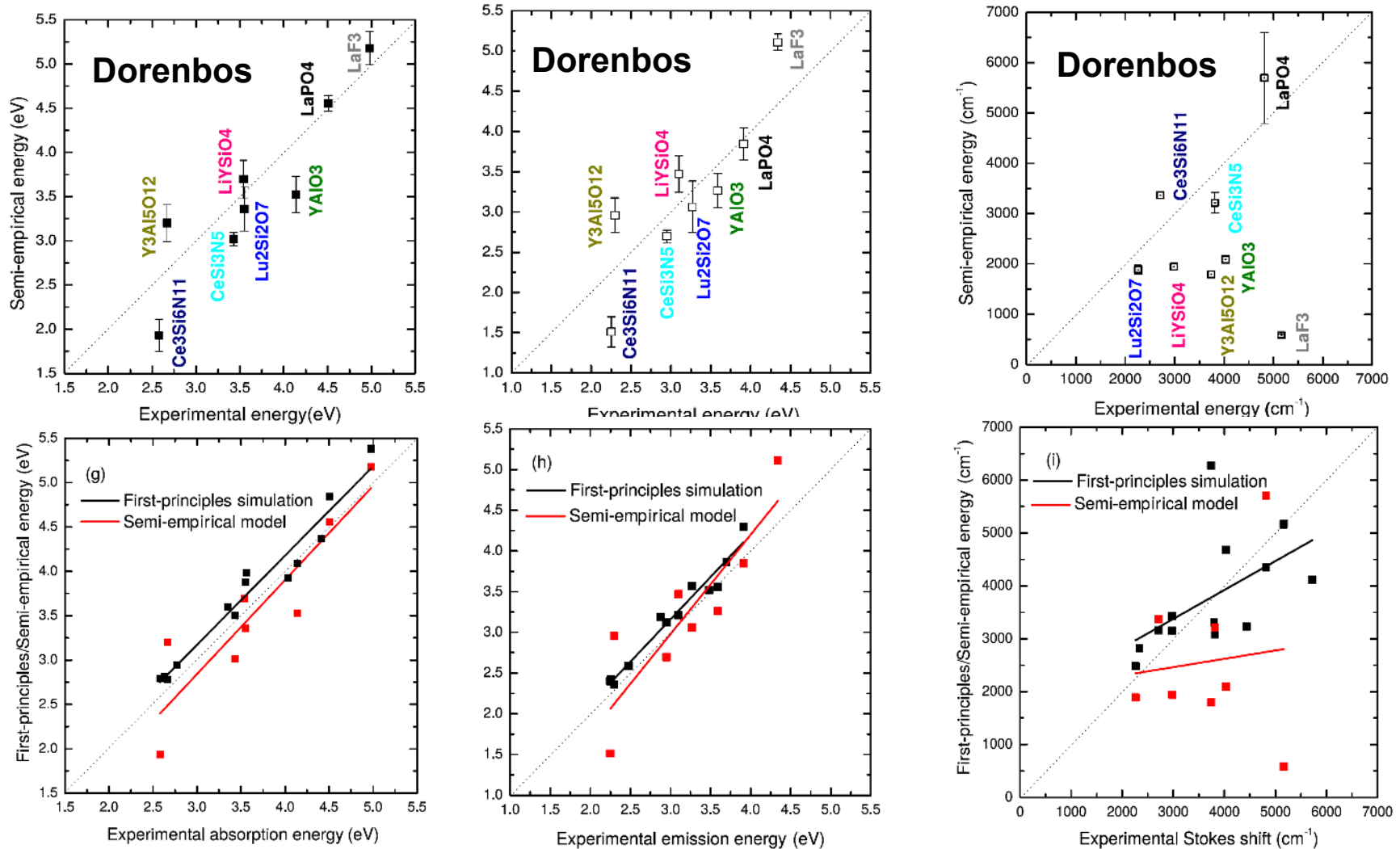
## First-principles



- First-principles absorption and emission energy are within 0.3 eV of experimental data, with two exceptions at 0.4 eV and 0.5 eV
- First-principles Stokes shifts are within 30%, except two values at 50%

Jia, Poncé, Miglio, Mikami & Gonze, *Adv. Opt. Materials*, 5, 1600997(2017)

# Using first-principles geometrical parameters in Dorenbos model : larger dispersion



Jia, Poncé, Miglio, Mikami & Gonze, Adv. Opt. Materials 1600997(2017)

# Statistical analysis

ME Mean Error  
 MAE Mean Absolute Error  
 MRE Mean Relative Error  
 MARE Mean Absolute Relative Error

	First-principles			Semi-empirical		
	Absorption	Emission	Stokes shift	Absorption	Emission	Stokes shift
ME	0.175 eV	0.205 eV	33.5 cm <sup>-1</sup>	-0.118 eV	0.027 eV	-1118 cm <sup>-1</sup>
MAE	0.205 eV	0.210 eV	728 cm <sup>-1</sup>	0.350 eV	0.423 eV	1502 cm <sup>-1</sup>
MRE (%)	5.100	6.280	4.17	3.540	-0.01	-26.7
MARE (%)	5.850	6.410	19.1	10.8	14.6	37.3
Slope	1.050	1.040	0.547	1.06	1.22	0.158
Intercept	0.156	0.038	1734	-0.034	-0.682	1989
R-Square (%)	95.10	96.10	25.00	78.8	72.3	-15.4

First-principle methodology clearly better than semi-empirical Dorenbos approach  
 Still, the latter has the correct trends, and single out important factors

Jia, Poncé, Miglio, Mikami & Gonze, *Adv. Opt. Materials*, 5, 1600997(2017)

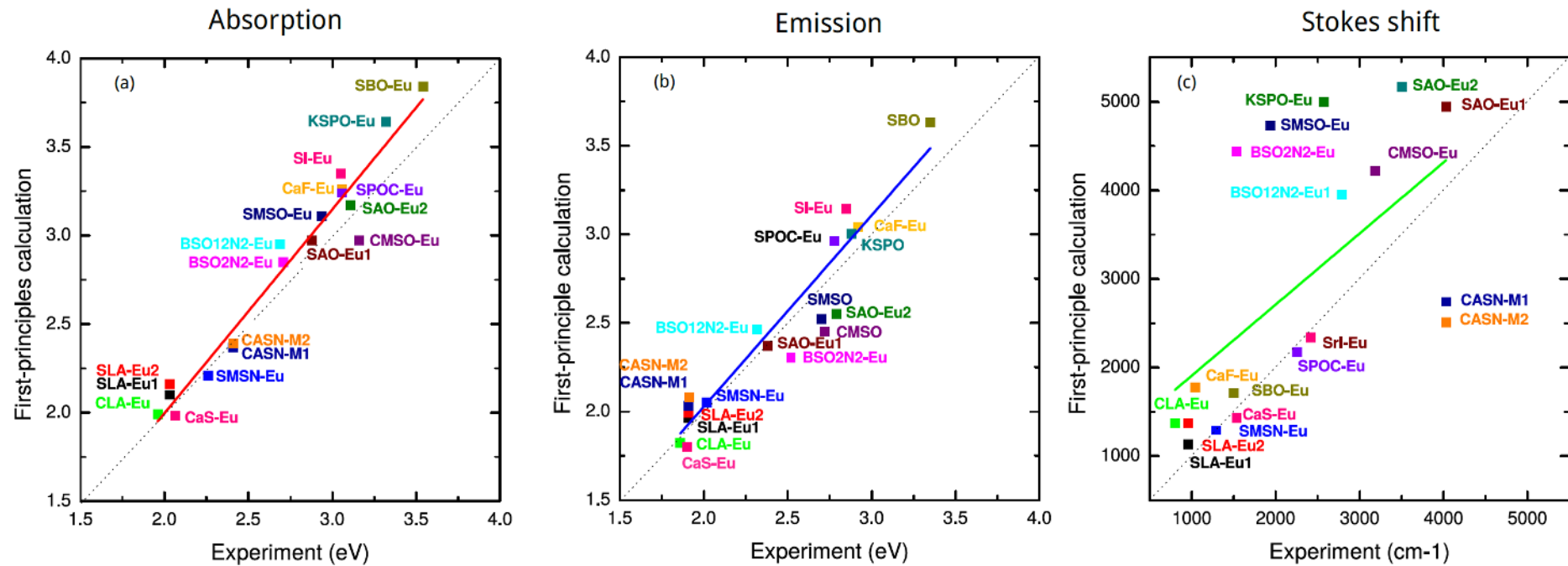
# Fifteen Eu-doped hosts covering 2-3.5 eV range

Compound	Calculation			Experiment		
	Abs	Em	$\Delta S$	Abs	Em	$\Delta S$
Sr[LiAl <sub>3</sub> N <sub>4</sub> ]:Eu1	2.10	1.96	1129	2.03	1.91	956
Sr[LiAl <sub>3</sub> N <sub>4</sub> ]:Eu2	2.16	1.99	1371	2.03	1.91	956
Ca[LiAl <sub>3</sub> N <sub>4</sub> ]:Eu	1.99	1.82	1371	1.96	1.86	800
Sr[Mg <sub>3</sub> SiN <sub>4</sub> ]:Eu	2.21	2.05	1290	2.26	2.02	1935
Ba <sub>3</sub> Si <sub>6</sub> O <sub>12</sub> N <sub>2</sub> :Eu	2.95	2.46	3952	2.69	2.32	2790
BaSi <sub>2</sub> O <sub>2</sub> N <sub>2</sub> :Eu	2.85	2.30	<b>4436</b>	2.71	2.52	1532
CaAlSiN <sub>3</sub> :Eu,M-I	2.37	2.03	2742	2.41	1.91	4032
CaAlSiN <sub>3</sub> :Eu,M-II	2.39	2.08	2508	2.41	1.91	4032
SrAl <sub>2</sub> O <sub>4</sub> :Eu1	2.97	2.37	4839	2.88	2.38	4033
SrAl <sub>2</sub> O <sub>4</sub> :Eu2	3.17	2.55	<b>4996</b>	3.11	2.79	2581
Sr <sub>5</sub> (PO <sub>4</sub> ) <sub>3</sub> Cl:Eu	3.24	2.96	2258	3.06	2.78	2178
SrI <sub>2</sub> :Eu	3.35	3.14	2339	3.05	2.85	2420
CaF <sub>2</sub> :Eu	3.26	3.04	1774	3.06	2.92	1047
CaS:Eu	1.97	1.80	1399	2.07	1.90	1466
SrBO <sub>4</sub> :Eu	3.84	3.63	1710	3.54	3.35	1502
Sr <sub>2</sub> MgSi <sub>2</sub> O <sub>7</sub> :Eu	3.11	2.52	<b>4726</b>	2.94	2.70	1936
CaMgSi <sub>2</sub> O <sub>6</sub> :Eu	2.97	2.45	4218	3.16	2.72	3188
KSrPO <sub>4</sub> :Eu	3.61	3.00	<b>4920</b>	3.32	2.88	3500

	First-principles		
	Absorption	Emission	Stokes shift
ME	0.104 eV	0.058 eV	428 cm <sup>-1</sup>
MAE	0.154 eV	0.159 eV	<b>819 cm<sup>-1</sup></b>
MRE (%)	3.55	2.27	33.7
MARE (%)	5.50	6.36	<b>44.2</b>
Slope	1.156	1.081	0.704
Intercept	-0.310	-0.135	1117
R-Square (%)	94.4	89.1	25.5

Jia, Poncé, Miglio, Mikami & Gonze, PRB 96, 125132 (2017).

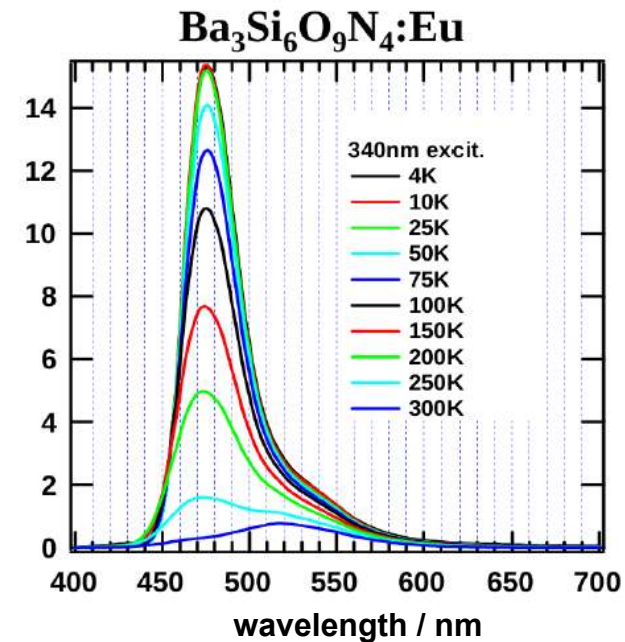
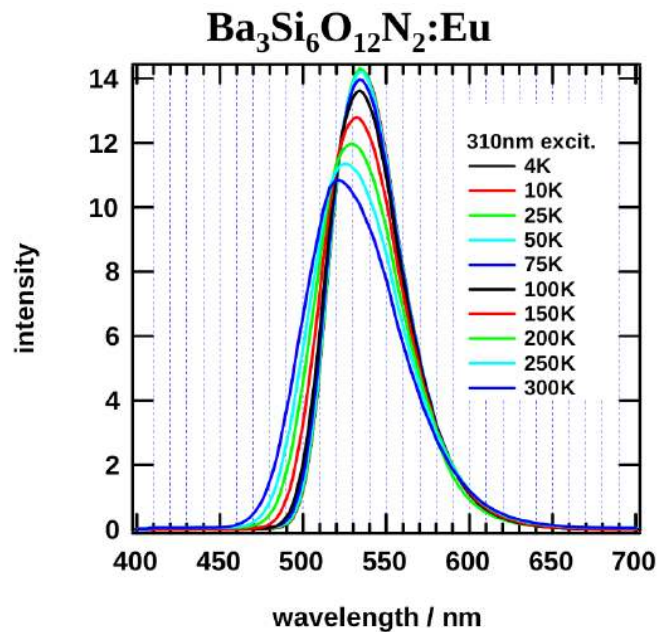
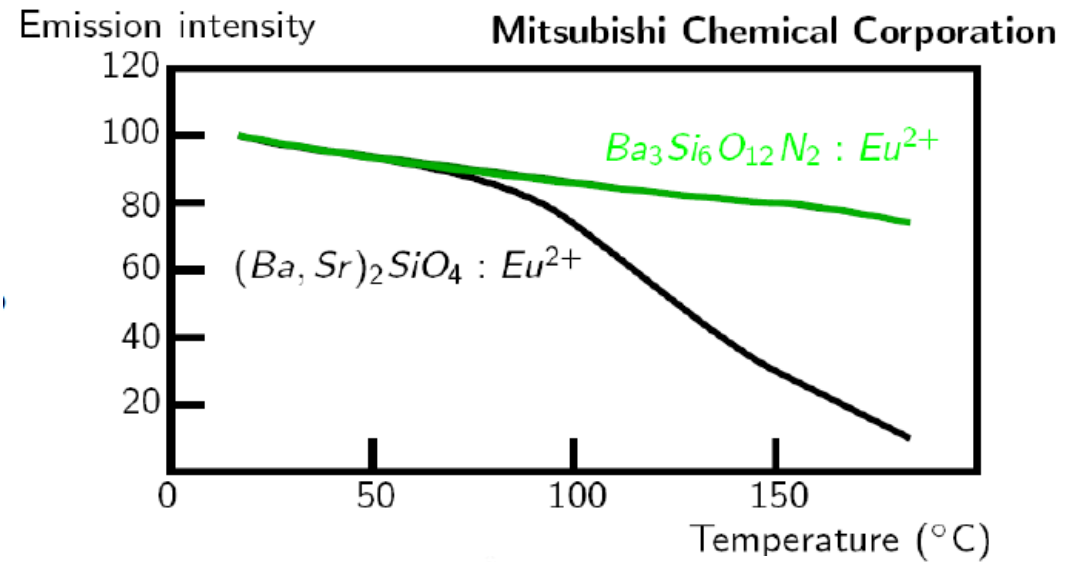
# Fifteen Eu-doped hosts covering 2-3.5 eV range



Jia, Poncé, Miglio, Mikami & Gonze, PRB 96, 125132 (2017).

# Thermal quenching ? Emission width ? The 1-D model and beyond

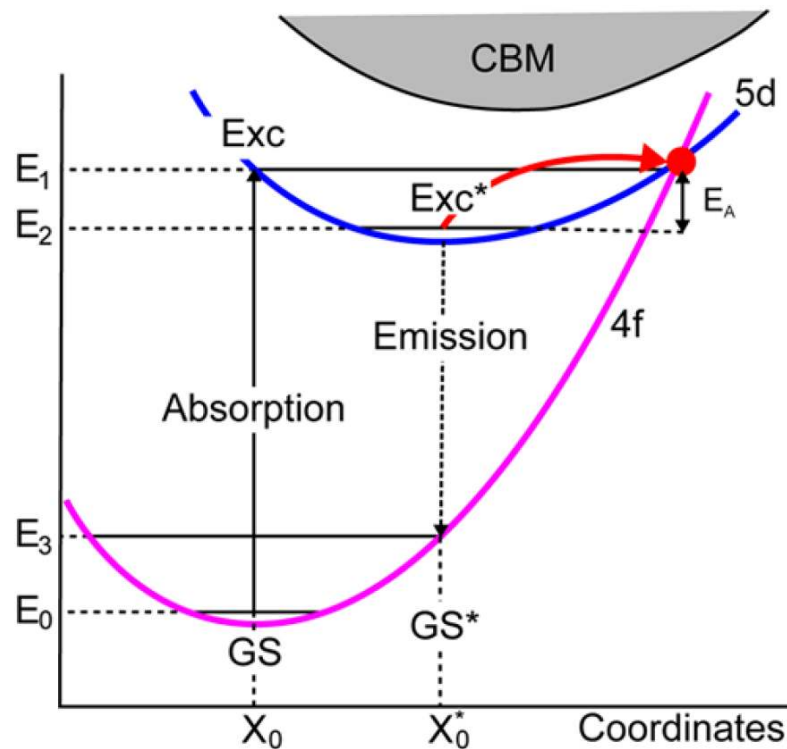
# Thermal quenching



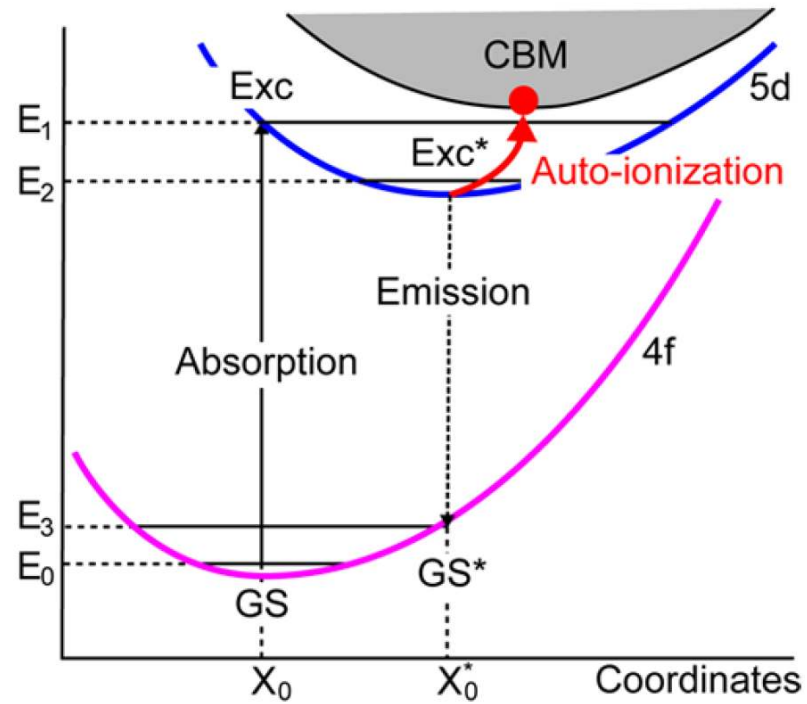
See e.g. C. Braun ... W. Schnick, Chem. Eur. J. 16, 9646 (2010)



# Models for thermal quenching



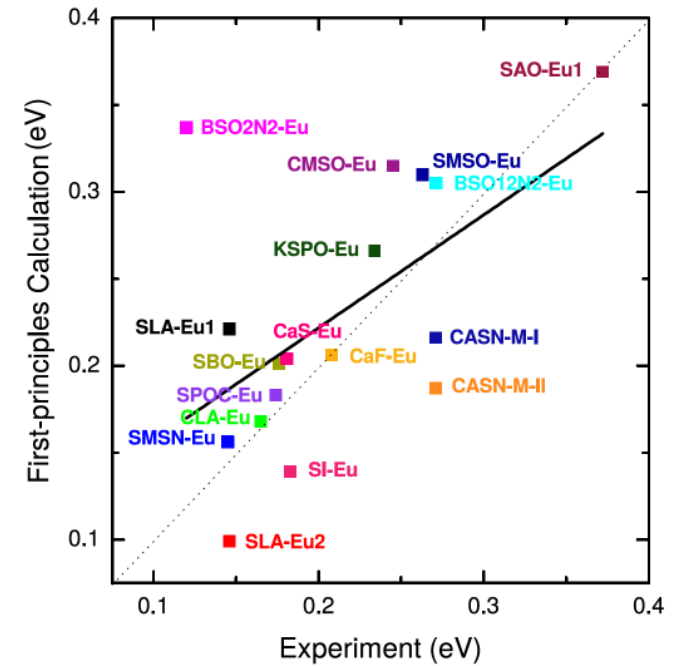
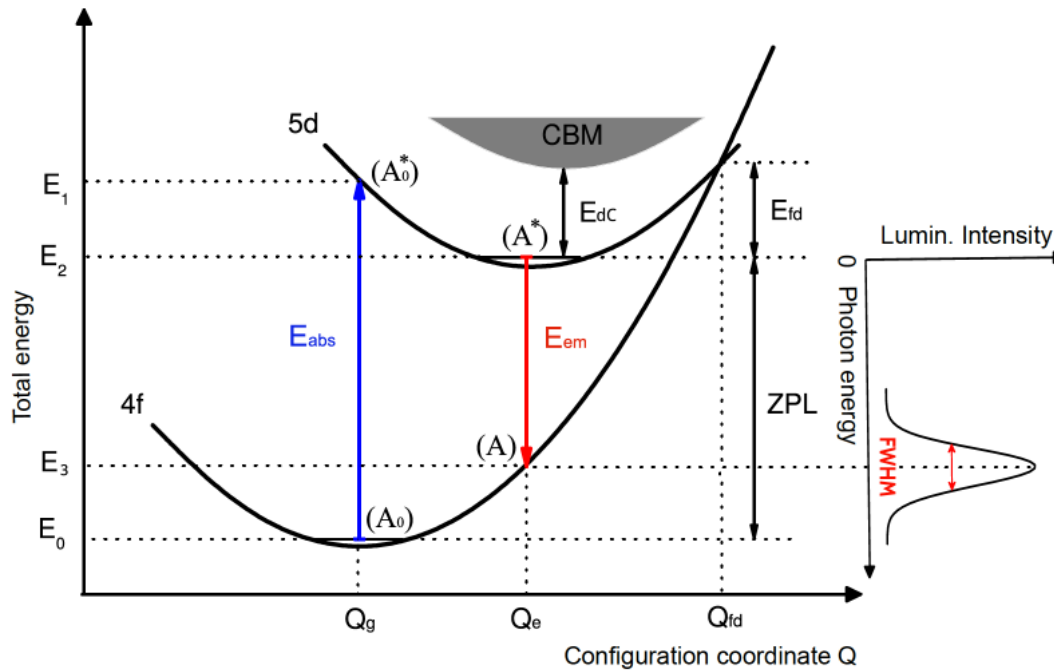
(a) 4f-5d crossing model



(b) Dorenbos auto-ionization model

- The 4f-5d energy barrier ( $E_A$ ) can be estimated in a 1-D picture + parabolic approximation, with only the usual 4 total energy calculations
- For the fifteen Eu-doped hosts, the energy barrier is estimated to be 1.9 eV or (much) larger. In favor of auto-ionization !

# Emission : Full width at half maximum



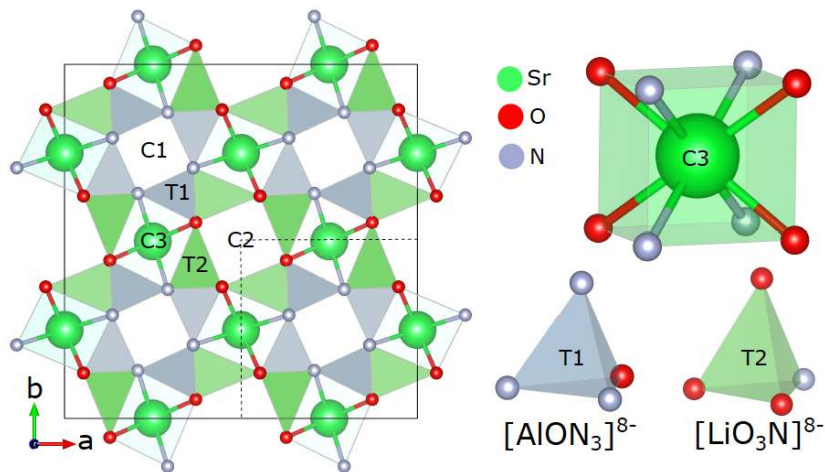
	First-principles calculation			
	Absorption	Emission	Stokes shift	FWHM
ME	0.104	0.058	428	0.018
MAE	0.154	0.159	819	0.046
MRE (%)	3.55	2.27	33.70	13.94
MARE (%)	5.50	6.36	44.2	26.81
Slope	1.156	1.081	0.704	0.650
Intercept	-0.310	-0.135	1117	0.092
R-Square (%)	94.4	89.1	25.5	26.7

Jia, Poncé, Miglio, Mikami & Gonze, PRB 96, 125132 (2017).

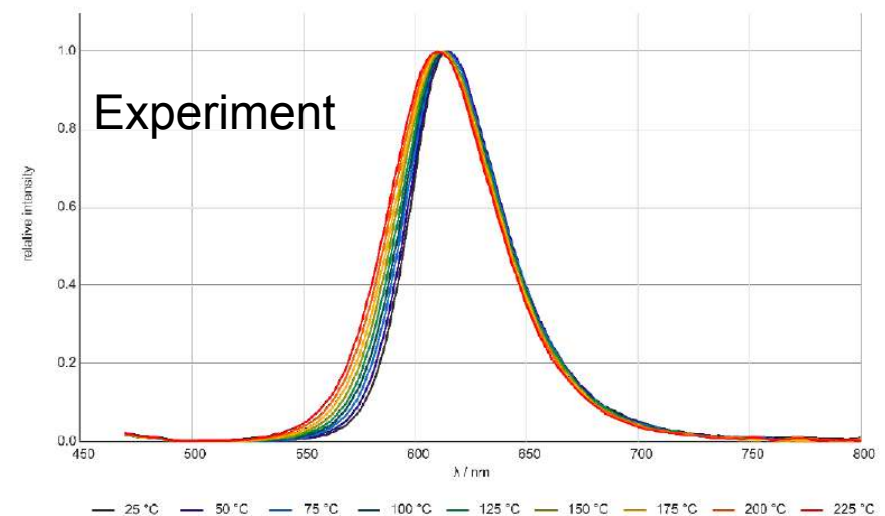
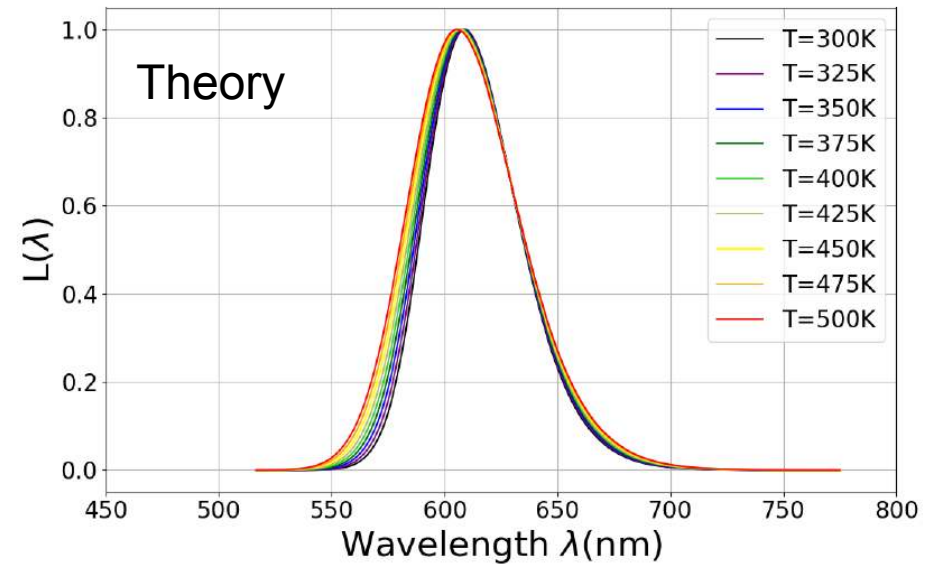
# Emission : shape/shift of the spectrum

Recently discovered  
 $\text{Sr}[\text{Li}_2\text{Al}_2\text{O}_2\text{N}_2]:\text{Eu}^{2+}$  phosphor

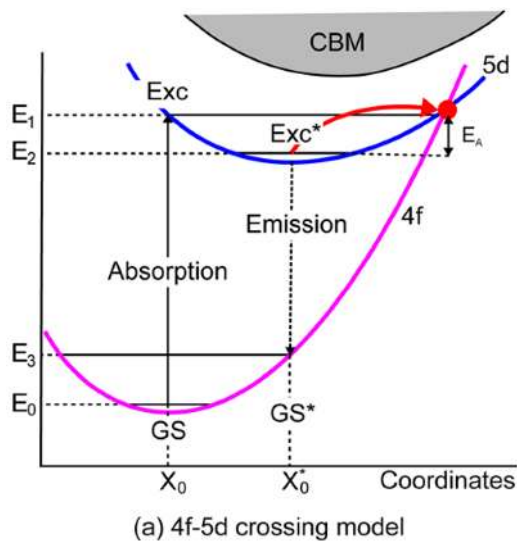
G.J. Hoerder et al, *Nature Comm.* 10, 1824 (2019)



J. Bouquiaux, Y. Jia, S. Poncé, A. Miglio, M. Mikami &  
 X. Gonze, *arXiv:cond-mat.mtrl-sci 2010:00423* (2020)  
 and in preparation



# Beyond the 1D model: 4f-5d crossing

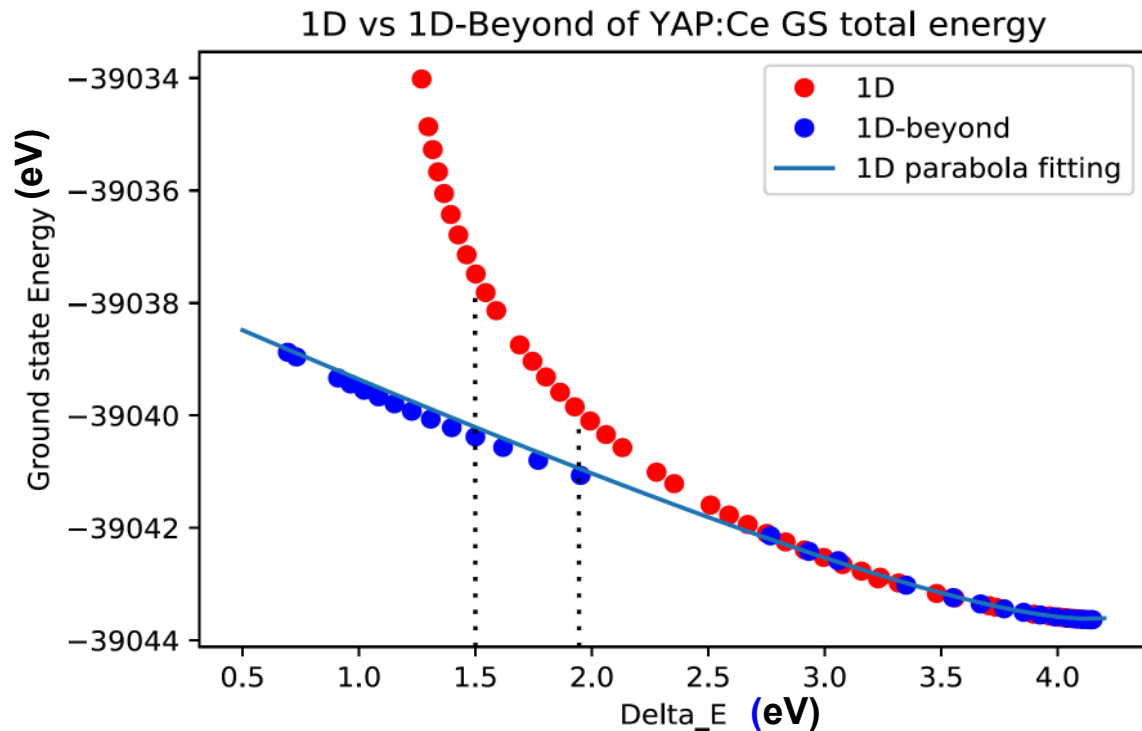


- More general statement of problem: in full coordinate space, find lowest  $E_A$  for a given  $\Delta E(5d-4f)$  (that might be zero)

- Adressed by Lagrange multiplier technique: geometry optimization on linked 4f and 5d systems

- Example for  $\text{YAlO}_3:\text{Ce}$
- Energy barrier is indeed lowered w.r.t. 1D model
- But not so much w.r.t parabolic approximation

Jia, Poncé, Miglio, Mikami & Gonze, *Phys. Rev. B* 100, 155109 (2019)



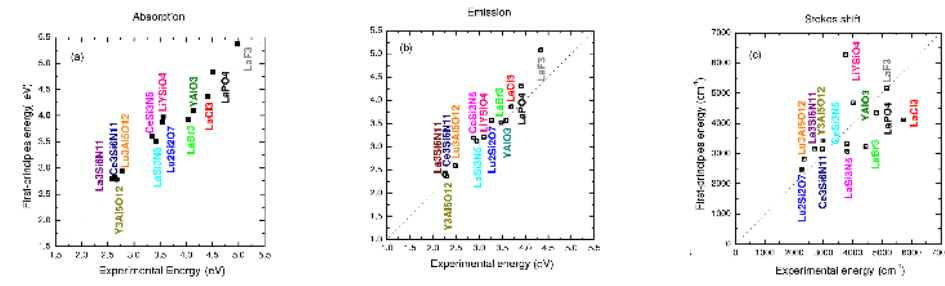
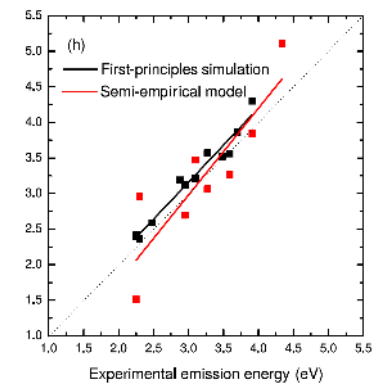
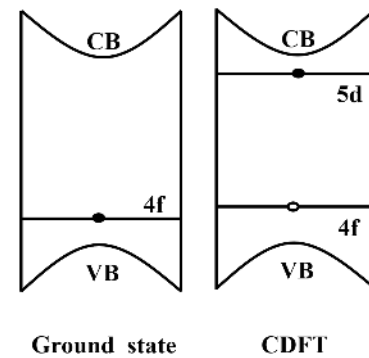
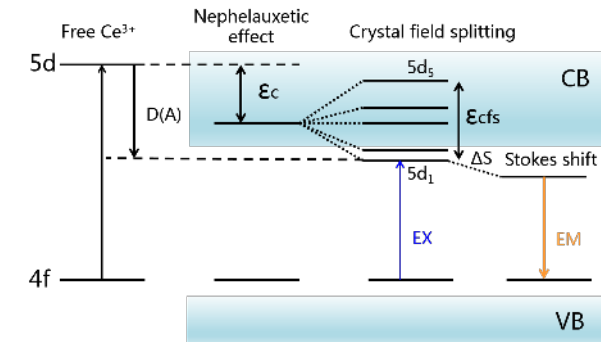
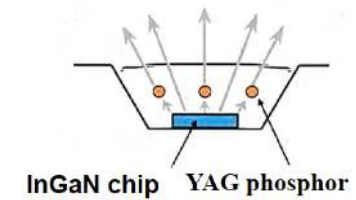
# Wrap-up

The most efficient white LEDs are phosphor-based :  
downconversion of blue light

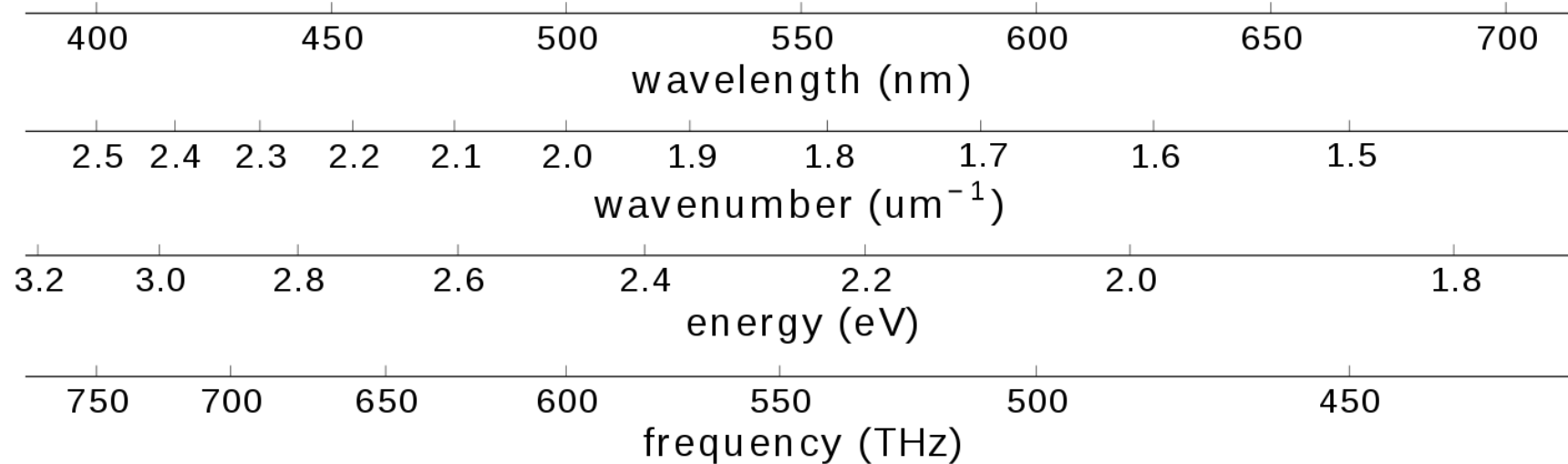
Need to optimize : Emission spectrum ;  
Excitation spectrum ; Quantum efficiency ;  
Optical characteristics at elevated temperature ; ...

Ce<sup>3+</sup> and Eu<sup>2+</sup> - doped inorganic hosts :  
tunable 4f – 5d transition

- First-principle methodology
- Absorption, emission & Stokes shift
- Study of 13 Ce-doped hosts and 18 Eu-doped hosts, to validate the methodology.
- Outperform the semi-empirical methodology (useful to get physical insights !)
- Thermal quenching & width



# Units for the visible spectrum



# Detailed information of semi-empirical fitting

Compounds	State	$\chi_{av}$	$\alpha_{sp}^i$	$\epsilon_c$	$\beta$	$R_{av}$	$\epsilon_{cfs}$	D(A)	D(A)	D(A)
								r=1.7	r=2.4	average
YAG:Ce	GS	1.425	2.694	13671cm <sup>-1</sup>	1.2×10 <sup>9</sup>	247.5pm	19614cm <sup>-1</sup>	25209cm <sup>-1</sup>	21844cm <sup>-1</sup>	23526cm <sup>-1</sup>
	EX	1.425	2.694	15253cm <sup>-1</sup>	1.2×10 <sup>9</sup>	243.1pm	20331cm <sup>-1</sup>	27212cm <sup>-1</sup>	23724cm <sup>-1</sup>	25468cm <sup>-1</sup>
LuAG:Ce	GS	1.483	2.514	17612cm <sup>-1</sup>	1.2×10 <sup>9</sup>	234.6pm	21803cm <sup>-1</sup>	30437cm <sup>-1</sup>	26697cm <sup>-1</sup>	28567cm <sup>-1</sup>
	EX	1.483	2.514	14446cm <sup>-1</sup>	1.2×10 <sup>9</sup>	242.3pm	20440cm <sup>-1</sup>	26470cm <sup>-1</sup>	22963cm <sup>-1</sup>	24717cm <sup>-1</sup>
LaPO <sub>4</sub> :Ce	GS	1.725	1.934	8403cm <sup>-1</sup>	5.67×10 <sup>8</sup>	260.3pm	8368cm <sup>-1</sup>	13325cm <sup>-1</sup>	11890cm <sup>-1</sup>	12608cm <sup>-1</sup>
	EX	1.725	1.934	8822cm <sup>-1</sup>	1.2×10 <sup>9</sup>	252.3pm	18875cm <sup>-1</sup>	19925cm <sup>-1</sup>	16687cm <sup>-1</sup>	18306cm <sup>-1</sup>
Lu <sub>2</sub> Si <sub>2</sub> O <sub>7</sub> :Ce	GS	1.543	2.346	10553cm <sup>-1</sup>	1.35×10 <sup>9</sup>	240.7pm	23301cm <sup>-1</sup>	24259cm <sup>-1</sup>	20262cm <sup>-1</sup>	22261cm <sup>-1</sup>
	EX	1.543	2.346	11938cm <sup>-1</sup>	1.35×10 <sup>9</sup>	235.7pm	24300cm <sup>-1</sup>	26232cm <sup>-1</sup>	22063cm <sup>-1</sup>	24148cm <sup>-1</sup>
LaSi <sub>3</sub> N <sub>5</sub> :Ce	GS	1.74	7.07	21380cm <sup>-1</sup>	5.67×10 <sup>8</sup>	281pm	7181cm <sup>-1</sup>	25604cm <sup>-1</sup>	24372cm <sup>-1</sup>	24988cm <sup>-1</sup>
	EX	1.74	7.07	23950cm <sup>-1</sup>	5.67×10 <sup>8</sup>	280pm	7232cm <sup>-1</sup>	28204cm <sup>-1</sup>	26963cm <sup>-1</sup>	27584cm <sup>-1</sup>
La <sub>3</sub> Si <sub>6</sub> N <sub>11</sub> :Ce	GS	1.68	7.52	25166cm <sup>-1</sup>	1.2×10 <sup>9</sup>	265pm	17088cm <sup>-1</sup>	35218cm <sup>-1</sup>	32286cm <sup>-1</sup>	33752cm <sup>-1</sup>
	EX	1.68	7.52	28242cm <sup>-1</sup>	1.20×10 <sup>9</sup>	260pm	17751cm <sup>-1</sup>	38683cm <sup>-1</sup>	35638cm <sup>-1</sup>	37161cm <sup>-1</sup>
CeSi <sub>3</sub> N <sub>5</sub>	GS	1.74	7.07	21445cm <sup>-1</sup>	5.67×10 <sup>8</sup>	280.8pm	7191cm <sup>-1</sup>	25675cm <sup>-1</sup>	24441cm <sup>-1</sup>	25058cm <sup>-1</sup>
	EX	1.74	7.07	23885cm <sup>-1</sup>	5.67×10 <sup>8</sup>	280.7pm	7196cm <sup>-1</sup>	28118cm <sup>-1</sup>	26883cm <sup>-1</sup>	27501cm <sup>-1</sup>
Ce <sub>3</sub> Si <sub>6</sub> N <sub>11</sub>	GS	1.69	7.46	25154cm <sup>-1</sup>	1.2×10 <sup>9</sup>	264.4pm	17166cm <sup>-1</sup>	35222cm <sup>-1</sup>	32306cm <sup>-1</sup>	33779cm <sup>-1</sup>
	EX	1.69	7.46	28198cm <sup>-1</sup>	1.20×10 <sup>9</sup>	259.6pm	17806cm <sup>-1</sup>	38672cm <sup>-1</sup>	35617cm <sup>-1</sup>	37145cm <sup>-1</sup>

# The bright present and future of blue and white LEDs

- blu-ray technology (high-density DVDs, laser printers)
- white lighting (public, home, industry, greenhouse, transportation...)
- dominant technology in back-illuminated liquid crystal displays (mobile phones, tablets, laptops, computer monitors, TV screens ...)

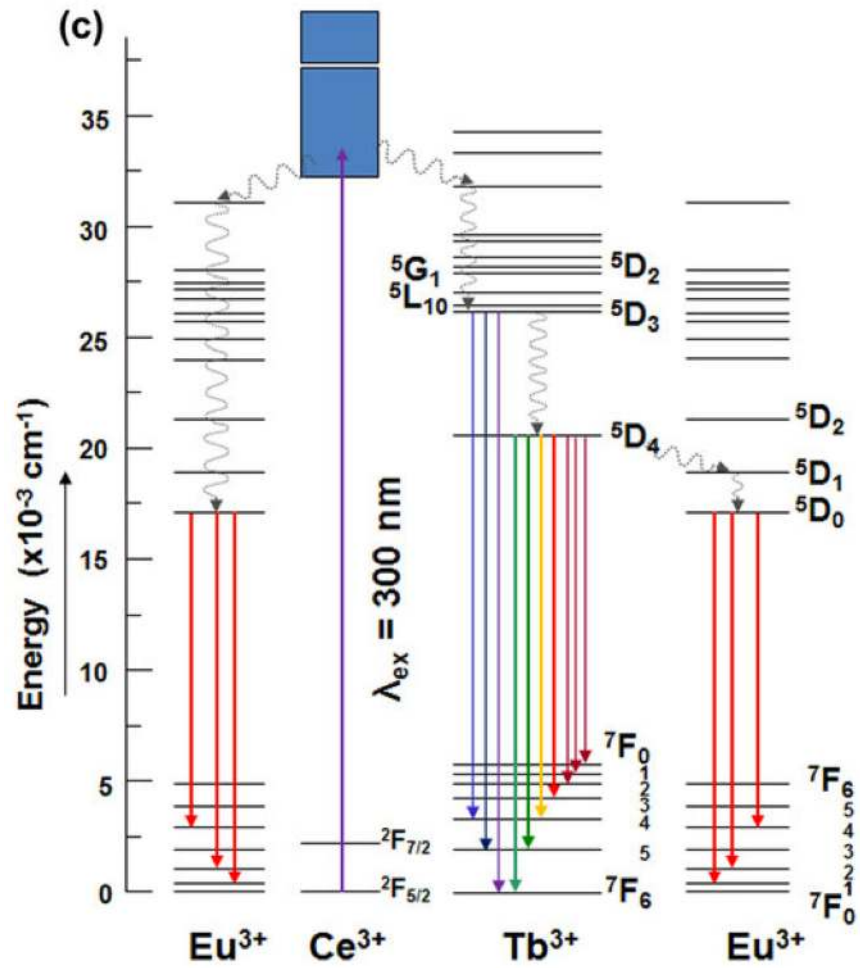
## Future

- UV for water purification
- Optical RGB white-LED wireless transmission (> 3 Gbits/sec)





# Excitation Spectra of Ce<sup>3+</sup> and Eu<sup>3+</sup>

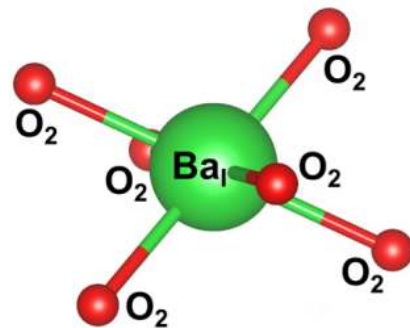


Important effect of spin-orbit coupling.

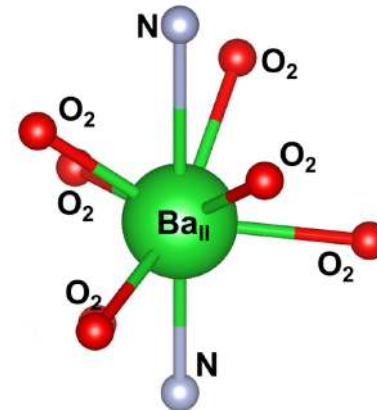
*Kim et al, Sci. Reports 5, 7866 (2015).*

# Geometry relaxation : $\text{Ba}_3\text{Si}_6\text{O}_{12}\text{N}_2$

	undoped <sup>b</sup>	ground state		excited state	
		Eu	diff %	Eu	diff %
$X_{\text{I}}-\text{O}_2$ (6×)	2.760	2.532	-8.3	2.388	-13.5
$X_{\text{II}}-\text{O}_2$ (3×)	2.959	2.869	-3.0	2.798	-5.4
$X_{\text{II}}-\text{O}_2$ (3×)	2.812	2.528	-10.1	2.352	-16.4
$X_{\text{II}}-\text{N}$ (1×)	3.054	2.878	-5.8	2.763	-9.5
$X_{\text{II}}-\text{N}$ (1×)	3.499	3.464	-1.0	3.578	2.3



(a)  $\text{Ba}_{\text{I}}$  in  $\text{Ba}_3\text{Si}_6\text{O}_{12}\text{N}_2$



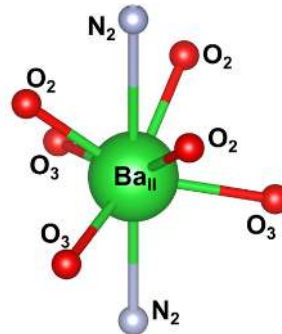
(b)  $\text{Ba}_{\text{II}}$  in  $\text{Ba}_3\text{Si}_6\text{O}_{12}\text{N}_2$

# Geometry relaxation : $\text{Ba}_3\text{Si}_6\text{O}_9\text{N}_4$

	undoped <sup>b</sup>	ground state		excited state	
		Eu	diff %	Eu	diff %
$X_I\text{-O}_2$ (3×)	2.714	2.561	-5.6	2.414	-11.0
$X_I\text{-O}_3$ (3×)	2.823	2.582	-8.5	2.489	-11.8
$X_I\text{-N}_1$ (3×)	3.498	3.729	6.6	3.768	7.7
$X_{II}\text{-O}_2$ (3×)	2.703	2.437	-9.8	2.343	-13.3
$X_{II}\text{-O}_3$ (3×)	2.860	2.758	-3.6	2.629	-8.1
$X_{II}\text{-N}_2$ (1×)	3.284	3.183	-3.1	3.059	-6.8
$X_{II}\text{-N}_2$ (1×)	3.579	3.469	-3.1	3.593	0.4
$X_{III}\text{-O}_2$ (3×)	2.730	2.535	-7.2	2.421	-11.3
$X_{III}\text{-O}_3$ (3×)	2.731	2.553	-6.5	2.450	-10.3
$X_{III}\text{-O}_1$ (3×)	3.375	3.579	6.0	3.388	0.4



(c)  $\text{Ba}_I$  in  $\text{Ba}_3\text{Si}_6\text{O}_9\text{N}_4$

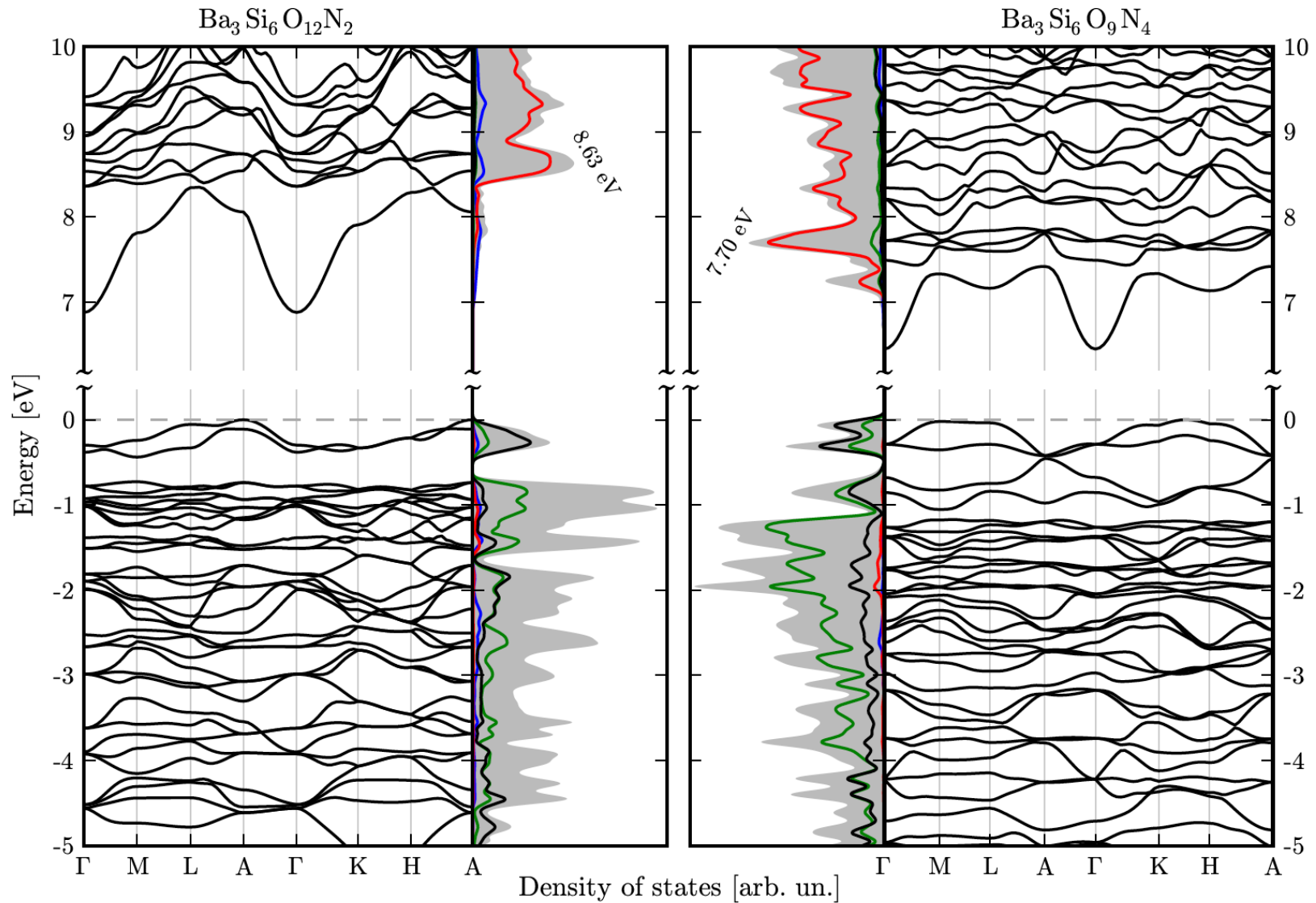


(d)  $\text{Ba}_{II}$  in  $\text{Ba}_3\text{Si}_6\text{O}_9\text{N}_4$

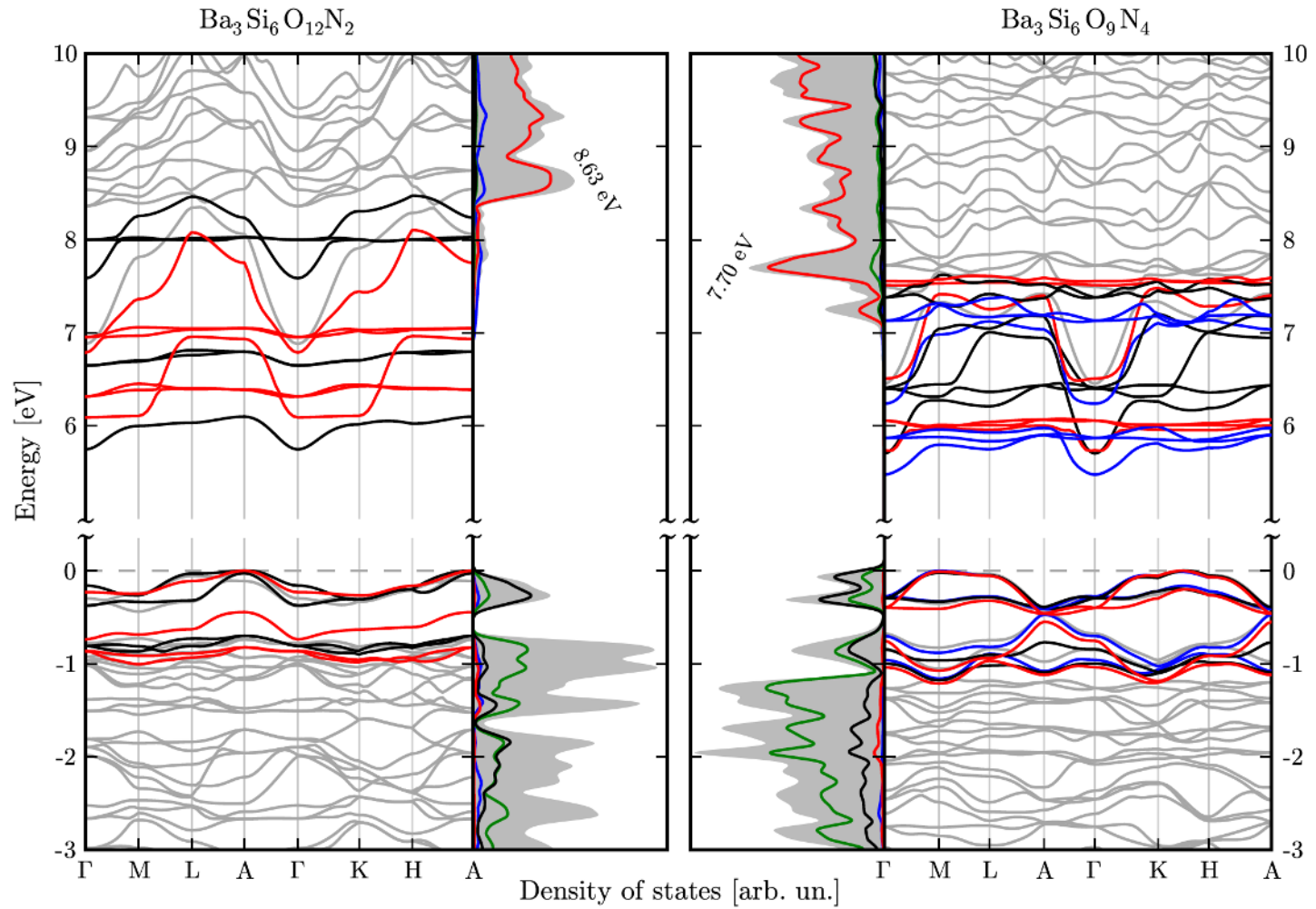


(e)  $\text{Ba}_{III}$  in  $\text{Ba}_3\text{Si}_6\text{O}_9\text{N}_4$

# Host band structure comparison (GW)



# Eu-doped band structure (excited state - GW)

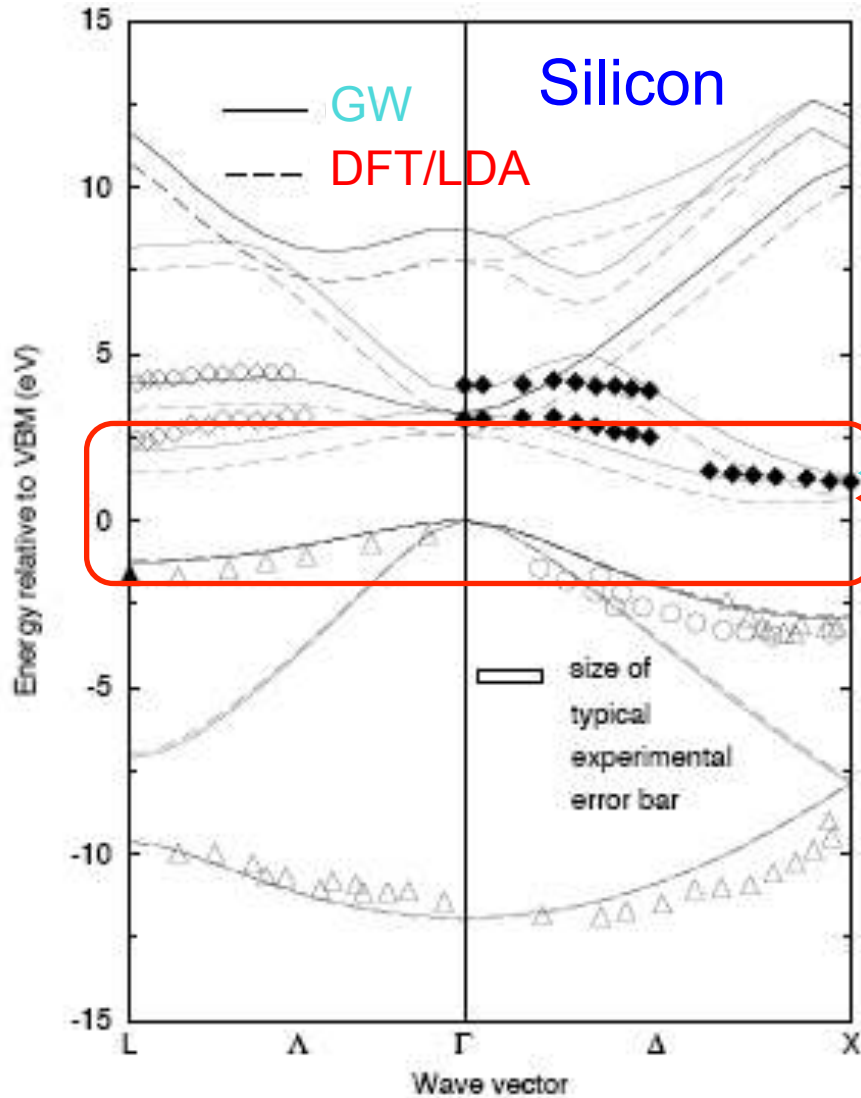


Black : Eu I  
 Red : Eu II

Absorption geometry,  
 primitive cell,  
 4f core-hole + GW0

Blue : Eu I  
 Black : Eu II  
 Red : Eu III

# The DFT bandgap problem



Comparison of **DFT/LDA** and **Many-Body Perturbation Theory GW** band structures with photoemission and inverse photoemission experiments for Silicon.

$E_g$  (GW)=1.2 eV

$E_g$  (DFT/LDA)=0.6 eV

$E_g$ (exp)=1.17 eV

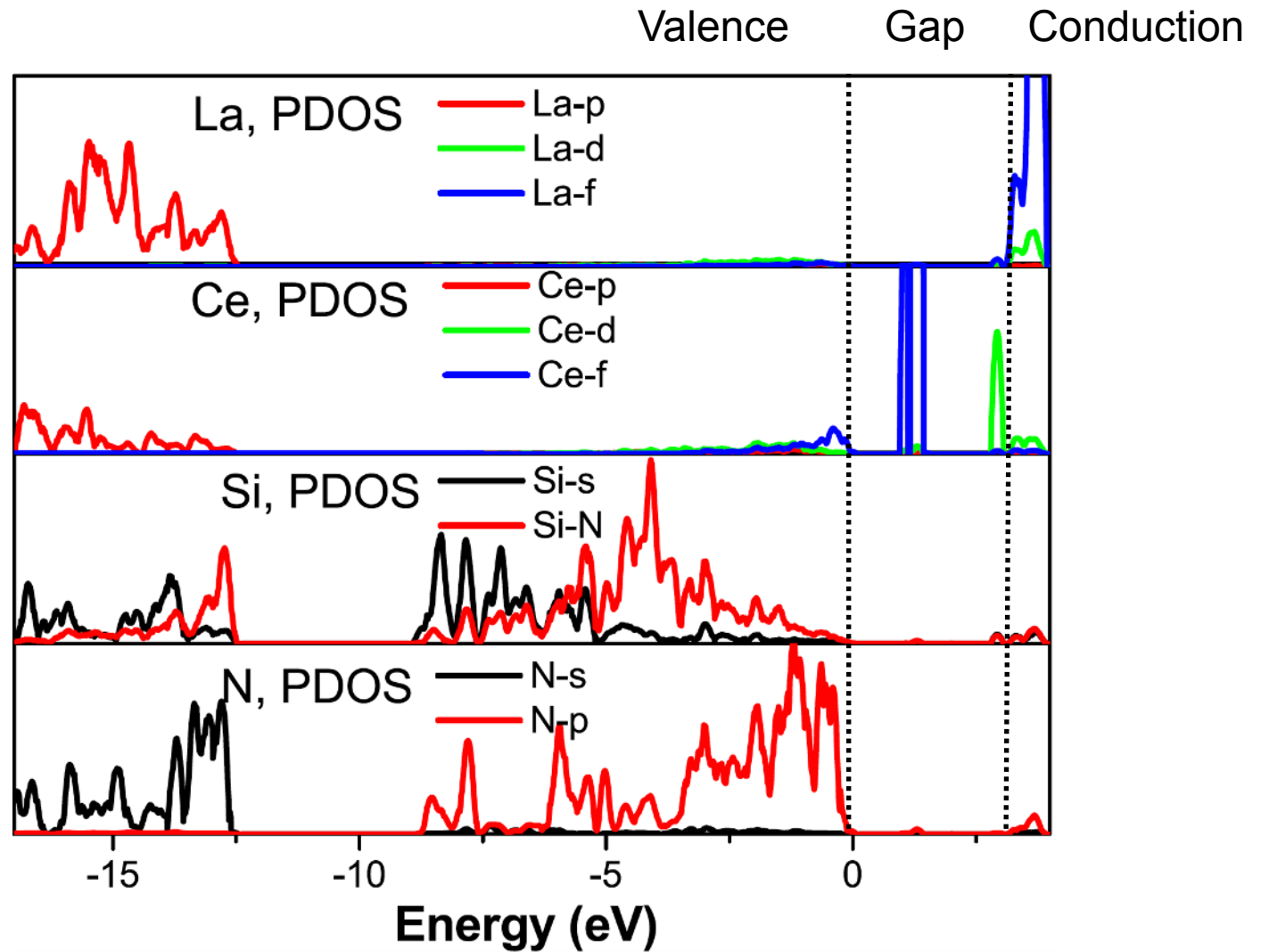
Problem !

*From "Quasiparticle calculations in solids",  
by Aulbur WG, Jonsson L, Wilkins JW,*

*Solid State Physics 54, 1-218 (2000)*

# La<sub>3</sub>Si<sub>6</sub>N<sub>11</sub>:Ce<sub>2a</sub> partial Density Of States

A\* case  
Excited-state  
Emission geometry



# Example : DOE Roadmap

A.1.3 Down Converters		
<p><b>Description:</b> Explore new regulatory compliant, high-efficiency wavelength conversion materials for improved quantum yield and phosphor conversion efficiency for the purposes of creating warm white LEDs, with a particular emphasis on improving spectral efficiency with high color quality and improved thermal stability. Non-REM (rare earth metal) down converters are encouraged.</p>		
Metric(s)	2011 Status(s)	2020 Target(s)
Quantum Yield (25°C) across the visible spectrum	90%	95%
Thermal Stability across the visible spectrum – Relative Quantum Yield @ 150°C vs. 25°C	90%	95%
Avg. Conversion Efficiency (pc-LED)	66%	69%
Spectral Full Width Half Max. (FWHM)	150 nm (Red)	<30 nm All colors
Color Stability (pc-LED)	Color Shift 0.012 u'v' over life	Color Shift < 0.002 u'v' over life
Spectral Efficiency relative to a max. LER ~345 lm/W	90%	100%
Flux Density @ 85°C		