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# Novel two-dimensional boron oxynitride predicted using the USPEX evolutionary algorithm†

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Oxidation is a unique process that significantly changes the structure and properties of a material. Doping of h-BN by oxygen is a hot topic in material science leading to the possibility of synthesis of novel 2D structures with customized electronic properties. It is still unclear how the atomic structure changes in the presence of external atoms during the oxidation of h-BN. We predict novel two-dimensional (2D) arrangements of boron oxynitride using the evolutionary algorithm of crystal structure prediction USPEX. All considered structures demonstrate semiconducting properties with a reduced bandgap compared with h-BN. Both molecular dynamics and phonon calculations show the dynamical stability of the new 2D B<sub>5</sub>N<sub>3</sub>O<sub>2</sub> phase, and our calculations demonstrate that it can form a bulk layered structure with an interlayer distance larger than that of pure h-BN. The optical characterization shows a redshift of the absorption spectrum compared with pure h-BN. Incorporation of oxygen into the structure of 2D BN during synthesis or oxidation can dramatically change the covalent network of h-BN while preserving its two-dimensionality and flatness, following the presence of local dipole moments which could improve the piezoelectric properties.

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## 1. Introduction

Chemically stable BN bulk materials can exist in four different polymorphic modifications: sp<sup>2</sup>-hybridized hexagonal (h-BN) and rhombohedral (r-BN), and sp<sup>3</sup>-hybridized cubic (c-BN) and wurtzite (w-BN).<sup>1–5</sup> Most promising among technological applications is h-BN<sup>6</sup> which attracts more attention due to its graphite-like layered crystal structure. While B and N atoms are held together by strong covalent bonds densely covering the plane, between BN layers there are only weak van der Waals forces. In contrast to graphene, BN has polar B–N bonds. BN nanoplates are known to preserve their thermal stability up to 1000 °C, undergoing oxidation in the range between 1000 and 1200 °C, with the formation of B<sub>2</sub>O<sub>3</sub>.<sup>7</sup>

From the practical point of view the use of h-BN in electronics is limited by wide band gap of ~5.5 eV.<sup>8–12</sup> Nevertheless, recent reports<sup>7,13</sup> state that oxygen doping of the monolayer h-BN

structure leads to reduction of band gap to 2.1 eV together with the observation of intriguing optical (fluorescence) and magnetic properties that depend on defect types. The defect chemistry of h-BN is most likely dominated by defects conditioned by impurities such as carbon, oxygen, and hydrogen. Substitutional carbon and oxygen, as well as interstitial hydrogen and boron vacancy–hydrogen complexes, are known as low-energy defects in h-BN.<sup>14</sup> The structure of oxidized boron nitride is based on the conception that the oxygen atoms incorporated in the h-BN lattice by replacing the nitrogen atoms. Such a way will provide a new practical method to control the electronic and magnetic properties of boron nitride.<sup>6</sup> It was shown by Weng *et al.*<sup>7</sup> that the band gap of h-BN may vary depending on the concentration of oxygen introduced into its crystal structure instead of nitrogen atoms with the maximum oxygen concentration of 23%. This allows to consider new bottom-up synthesis routes and incorporation of two-color fluorescent boron oxynitride nanodots into a hybrid organic–inorganic film.<sup>15</sup> In fact, theoretical modeling confirmed that the band gap of BN nanosheets and BN nanotubes can be significantly reduced by replacement of nitrogen atoms by oxygen atoms.<sup>16,17</sup> Similarly, the optical, electronic, and magnetic properties can be tuned as has been predicted in numerous theoretical works, *i.e.* ref. 17–19. Previous experimental studies using ring dark field scanning transmission microscopy demonstrate that the presence of oxygen atoms in the h-BN lattice is truly possible.<sup>20</sup>

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Thus, the oxidized boron nitride could be a promising material for further investigations and applications, because it is still unclear how the atomic structure changes in the presence of external atoms during the oxidation of h-BN. This motivated us to study the crystal structures of B–N–O by using the evolutionary structure prediction of two-dimensional materials.<sup>21</sup>

## II. Methods

The search for thermodynamically stable 2D compounds in the B–N–O system was performed using the variable-composition evolutionary search as implemented in the USPEX code.<sup>22–24</sup> The thickness of 2D crystals is restricted in a range of 0–6 Å, and the total number of atoms is specified to be 8–18. The initial population of 180 structures were generated using a random symmetric structure generator,<sup>24</sup> while the subsequent generation contains 120 structures, 20% of which were produced using a random symmetric structure generator, and 80% by variation operators (heredity, soft mutation, and atomic transmutation).

All structures were relaxed using the density functional theory (DFT).<sup>25,26</sup> The generalized gradient approximation (GGA) method was used with the Perdew–Burke–Ernzerhof (PBE) parameterization for the exchange–correlation functional,<sup>27</sup> implemented in the VASP package.<sup>28–31</sup> For bulk structures, van der Waals interactions were taken into account using the Grimme correction.<sup>32</sup> The cutoff energy of plane waves was set to 500 eV. The sampling of the Brillouin zone was done using a uniform *k*-point grid with a resolution of  $2\pi \times 0.5 \text{ \AA}^{-1}$ .

To study the stability of the predicted phases, we computed their energy of formation:

$$E_f = \frac{E_{\text{BNO}} - n\mu_{\text{B}} - m\mu_{\text{N}} - p\mu_{\text{O}}}{N}$$

where  $E_{\text{BNO}}$  is the total energy of the predicted structure;  $\mu_{\text{B}}$ ,  $\mu_{\text{N}}$ , and  $\mu_{\text{O}}$  are the chemical potentials of atoms calculated for *a*-B, molecular nitrogen, and oxygen; *n*, *m*, and *p* are the number of boron, nitrogen, and oxygen atoms; and *N* is the total number of atoms in the system.

The phonon dispersion curves of the predicted structures were calculated using the finite displacement method as implemented in the PHONOPY code.<sup>33</sup>

The extinction coefficient was calculated using the superposition of the Lorentz oscillators to simulate the complex dielectric function depending on the frequency of light. The real part was determined using the Kramers–Kronig relations, the imaginary part was found by summing over the unfilled states.<sup>34</sup> In terms of the dielectric function, the extinction coefficient is

$$K(\lambda) = \left[ \frac{\sqrt{\varepsilon_1^2 + \varepsilon_2^2} - \varepsilon_1}{2} \right]^{1/2}$$

We applied the *ab initio* molecular dynamics (AIMD) to the B–N–O structures to study their dynamical and thermal stability using a  $2 \times 2 \times 1$  supercell. The molecular dynamics simulations were carried out at constant temperatures of 600 and 1200 K

using the Nosé–Hoover thermostat.<sup>35,36</sup> The total time of the simulations was set to 3.5 ps, which is enough to observe critical changes in the atomic structure, with a time step of 1 fs. The atomic structure was recorded after every 10 ionic steps.

## III. Results and discussion

### Crystal structure prediction

On the basis of the experimental data,<sup>7</sup> the composition of boron nitride nanosheets with oxygen doping (44.7% of boron, 30.7% of nitrogen, 23.1% of oxygen, 1.5% of other impurities) was set as the starting point for structure prediction. We predicted new two-dimensional structures based on h-BN doped by oxygen atoms with the general formula  $\text{B}_x\text{N}_y\text{O}_z$ , where *x*, *y*, and *z* are the number of boron, nitrogen, and oxygen atoms in the unit cell, respectively. Two types of structures were considered: (i) those with the sum of the N and O atoms equal to the number of the B atoms ( $x = y + z$ ), to simulate ternary systems obtained using the growth mechanism, and (ii) those with an equal number of the B and N atoms ( $x = y$ ), to simulate ternary systems created by oxygen doping of h-BN (Fig. 1a and b).

Fig. 1a shows the case (i) results of the search for B–N–O structures with fixed compositions at different oxygen concentrations. For N-rich structures (*e.g.*,  $\text{B}_3\text{N}_4\text{O}$ ) with an oxygen concentration of 17%, we obtained a monolayer  $\text{B}_3\text{N}_2\text{O}$  structure with separate  $\text{N}_2$  molecules near the surface. These results confirm that substitution of B would cause structural deformations and instability of a BN sheet.<sup>16</sup>

It was found that  $\text{B}_4\text{N}_3\text{O}$  and  $\text{B}_3\text{N}_2\text{O}$  compositions (Fig. 1a) have a structure of h-BN with oxygen replacing some nitrogen atoms. Increasing the oxygen concentration, defined as the number of the oxygen atoms related to the total number of atoms in the B–N–O structure, to 20% ( $\text{B}_5\text{N}_3\text{O}_2$ ) leads to the formation of another structure with 5 to 11 periodically arranged defects along the *y* axis, which are separated by a line of 6-member rings along the *x* axis (Fig. 1a). Importantly, the oxygen concentration in  $\text{B}_5\text{N}_3\text{O}_2$  is close to that of the experimental composition.<sup>7</sup> To compare the calculation results with the experimental data, we estimated the total energy and interlayer distance in the layered bulk structure of  $\text{B}_5\text{N}_3\text{O}_2$  and pure h-BN. The interlayer distance of bulk  $\text{B}_5\text{N}_3\text{O}_2$  was found to be larger than that of h-BN (3.42 vs. 3.23 Å), which agrees with the experimental data.<sup>7</sup>

Then we applied an evolutionary algorithm to predict the B–N–O compositions with an equal number of boron and nitrogen atoms. Studying the possibility of formation of 2D B–N–O structures *via* oxygen doping of h-BN, we predicted  $\text{B}_3\text{N}_3\text{O}$ ,  $\text{B}_4\text{N}_4\text{O}$ ,  $\text{B}_6\text{N}_6\text{O}$ , and  $\text{B}_8\text{N}_8\text{O}$  compositions using the USPEX algorithm. Fig. 1b shows the geometry of these lowest-energy  $\text{B}_x\text{N}_x\text{O}$  ( $x = 3, 4, 6, 8$ ) nanostructures. Oxidation of h-BN led to formation of 2D materials with unique structures differing from that of h-BN. For clarity, in Fig. 1b the polygons forming unit cells are painted in different colors: *n*-angle polygons ( $n = 4, 5, 6, 7, 8, \dots$ ) are shown in yellow, blue, green, red, orange, and gray, respectively. The structures with a higher

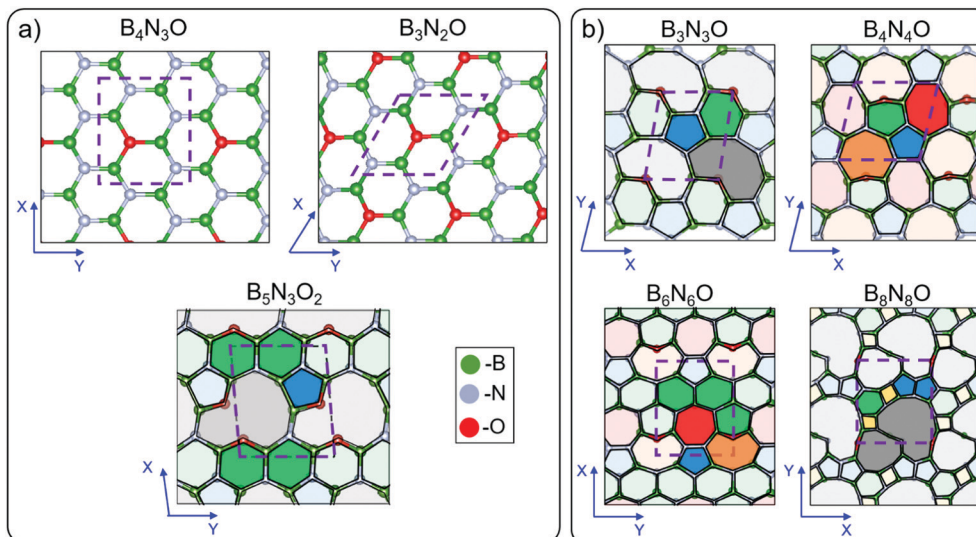


Fig. 1 Predicted  $B_xN_yO_z$  structures with (a)  $x = y + z$  and (b)  $x = y$ . The boron, nitrogen, and oxygen atoms are shown in green, gray, and red, respectively.

oxygen concentration,  $B_3N_3O$  and  $B_4N_4O$ , in addition to 6-member formations also have 5-atom ones with a homoatomic bond between the nitrogen atoms. The oxygen atoms are often located in 6-member rings, which are adjacent to polygons with 8, 9 and larger number of vertices.

To check the stability of the predicted B–N–O structures, we calculated the ternary phase diagram (Fig. 2). Because bulk layered materials always have a lower energy than their 2D counterparts, we used only two-dimensional structures to construct the ternary phase diagram except the elemental structures of boron, oxygen, and nitrogen. For this reason, bulk  $B_2O_3$  was not considered, whereas the structures of two-dimensional stoichiometric boron oxides<sup>37</sup> were taken into account. It was found that the B–N–O structures with an equal number of the boron and nitrogen atoms have the energy of

formation about 1.5 times lower in absolute value than the structures with the chemical ratio of  $x = y + z$  ( $B_5N_3O_2$ ,  $B_3N_2O$ , and  $B_4N_3O$ ). The  $B_5N_3O_2$  structure has the lowest formation energy among all considered 2D B–N–O structures, even in comparison with h-BN, which makes it thermodynamically stable (Fig. 2). Increasing the concentration of oxygen leads to the formation of structures associated with nitrogen-doped boron oxides rather than oxidized boron nitrides.

At low concentrations of oxygen, defective and low-density structures  $B_6N_6O$  and  $B_8N_8O$  are formed, containing a large variety of polygonal rings in the unit cell, including 4-, 7-, 8-, and 12-member rings interconnected with boron nitride hexagons.

### Stability of $B_5N_3O_2$

To investigate the dynamical stability of  $B_5N_3O_2$ , both the phonon dispersion calculations and molecular dynamics simulations were performed. The phonon dispersion (Fig. S1a, ESI<sup>†</sup>) shows that none of the acoustic vibrational modes is imaginary (both LA and TA are real) except the out-of-plane acoustic mode (ZA) mainly associated with long-range out-of-plane corrugations. The calculations of the phonon dispersion with different sizes of supercells show the trend toward vanishing of the imaginary part. The imaginary frequency of the ZA mode at the  $\Gamma$ -point (Fig. S1a, ESI<sup>†</sup>), comes from the lack of consideration of the rotational invariance.<sup>38,39</sup> Imposing the translational and rotational invariances, which is crucial for an accurate description of phonons in any 2D system, leads to vanishing of the imaginary frequency part of the ZA mode (Fig. S1b, ESI<sup>†</sup>). A detailed physical insight is presented in the ESI<sup>†</sup>.

*Ab initio* molecular dynamics (AIMD) simulations can show the origin of the imaginary mode in the phonon dispersion. Fig. 3 shows the oscillations of the total energy of  $B_5N_3O_2$  at 600 and 1200 K. The energy is given with respect to the ground state ( $E_{\min}$ ) at 0 K. In Fig. 3 the side and top views of the atomic structure at 3 ps and 1200 K are shown. Both the energy

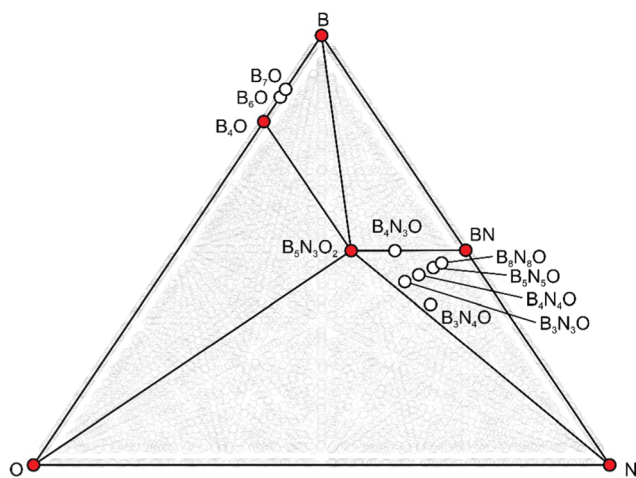


Fig. 2 Ternary phase diagram of the two-dimensional B–N–O structures in the formation energy and composition coordinates. Thermodynamically stable and metastable structures are shown by red and white circles, respectively.

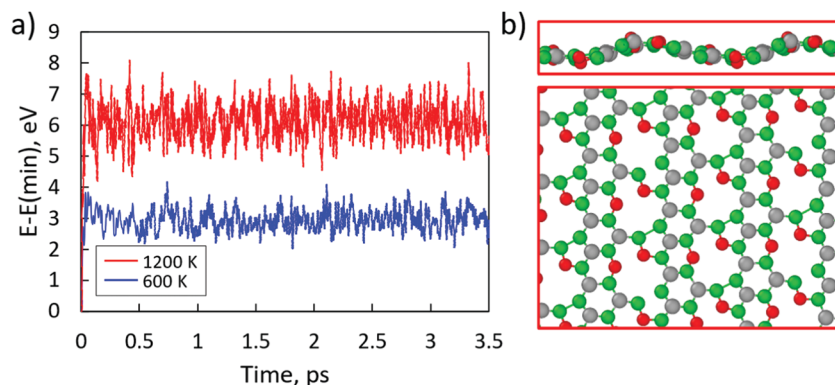


Fig. 3 Thermal stability of  $B_5N_3O_2$  at finite temperatures. (a) Fluctuations of the potential energy ( $2 \times 2 \times 1$  supercell) during the NVT *ab initio* MD simulations at 600 K (blue) and 1200 K (red). (b) Side and top views of the atomic structure at 3 ps and 1200 K. The boron, nitrogen, and oxygen atoms are shown in green, gray, and red, respectively.

oscillations and structure visualizations show dynamical stability of  $B_5N_3O_2$ . We assume that the out-of-plane corrugations that appeared because of the thermal motion (Fig. 3b, top panel) can be responsible for potential dynamical instability and the presence of imaginary modes in the phonon dispersion (the calculations of the phonon dispersion were carried out for an atomically flat structure). The AIMD simulations for other B–N–O structures predicted in this study are presented in Fig. S2 (ESI<sup>†</sup>).

In the B–N–O structures considered in this study, the number of various polygonal cycles rises as the oxygen concentration decreases. On the other hand, a decrease in the oxygen concentration should lead to dominance of the hexagonal structure of boron nitride, with oxygen replacing some nitrogen atoms or absorbing at the surface. In combination with the phonon dispersion results, this allows us to assert the stability of  $B_5N_3O_2$ .

### Electronic and elastic properties of 2D boron oxynitride nanosheets

The calculation of the electronic properties of  $B_5N_3O_2$  shows a decrease of the bandgap down to 3.0 eV based on PBE<sup>27</sup> calculations (Fig. S3a, ESI<sup>†</sup>), which is much smaller than for pure boron nitride and lower than that of the structures studied in previous works.<sup>7</sup> The main contribution in the top of valence bands comes from whole atoms B, N and O, but the bottom of conduction bands filled mainly by boron atoms similar to h-BN,<sup>40</sup> where the valence band is formed by a more electronegative nitrogen, while the conduction band is formed by less electronegative boron. The hybrid HSE06 functional expand the band gap value up to 4.4 eV (Fig. S3b, ESI<sup>†</sup>). The contribution of oxygen near the bandgap is equal to nitrogen, which indicates that the bandgap decrease is caused by the peculiarities of the two-dimensional crystal structure—the formation of non-hexagonal cycles in whole range of B–N–O structures (Fig. S4, ESI<sup>†</sup>). Additionally, to make a more accurate comparison, the Kubelka–Munk plot for  $B_5N_3O_2$  was performed (Fig. S5 in the ESI<sup>†</sup>). The obtained direct optical band gap were estimated to be 2.9 eV and 2.5 eV for the longitudinal and transverse

directions. It should be noted that the obtained greater value of the band gap in comparison with the experimental data are caused by the consideration of periodic BNO structures, while the band gap decrease is mainly caused by the presence of edge states due to the finite size of synthesized sample<sup>7</sup> as well as in pure h-BN, the formation of the edges leads to a decrease in the value of the band gap.<sup>41</sup> The results indicate the potential of using oxygen to obtain new semiconducting 2D materials based on the h-BN lattice.

Because the new materials are based on h-BN, we expected them to exhibit comparable mechanical properties. For all the predicted B–N–O structures, we estimated elastic constants using the stress–strain relations  $\sigma_i = C_{ij}\eta_j$ , where  $\sigma_i$  is *i*th component of the stress tensor,  $C_{ij}$  is the elastic tensor,  $\eta_j$  is *i*th component of the deformation tensor. The value of each elastic constant was determined as the slope of the obtained

Table 1 Elastic constants of 2D materials

	$C_{11}$ (N m <sup>-1</sup> )	$C_{12}$ (N m <sup>-1</sup> )	$C_{22}$ (N m <sup>-1</sup> )	$C_{44}$ (N m <sup>-1</sup> )
$B_5N_3O_2$	201.8	6.9	75.7	57.28
BNO (20 atom %) <sup>7</sup>	217.39	73.57	224.82	
BNO (10 atom %) <sup>7</sup>	235.34	65.957	240.29	
BC <sub>2</sub> N(I) <sup>7</sup>	263.50	46.387	283.62	
BC <sub>2</sub> N(II) <sup>7</sup>	292.73	51.744	283.25	
Graphene	342 <sup>43</sup>			
	345 <sup>44</sup>	64.1 <sup>48</sup>		143.75 <sup>48</sup>
	347.2 <sup>45</sup>			
	348 <sup>46</sup>			
	335 <sup>47</sup>			
	351.6 <sup>48</sup>			
h-BN	271 <sup>44</sup>			
	291.3 <sup>45</sup>			
	267 <sup>47</sup>			
WS <sub>2</sub>	148.47 <sup>48</sup>	31.2 <sup>48</sup>		58.63 <sup>48</sup>
	137 <sup>49</sup>	31.8 <sup>50</sup>		
	146.5 <sup>50</sup>	31.0 <sup>51</sup>		
	144.0 <sup>51</sup>			
	151.48 <sup>52</sup>			
MoS <sub>2</sub>	134.89 <sup>48</sup>	32.03 <sup>48</sup>		51.43 <sup>48</sup>
	123 <sup>49</sup>	33.0 <sup>50</sup>		
	132.7 <sup>50</sup>	32.6 <sup>51</sup>		
	128.4 <sup>51</sup>			
	138.12 <sup>52</sup>			

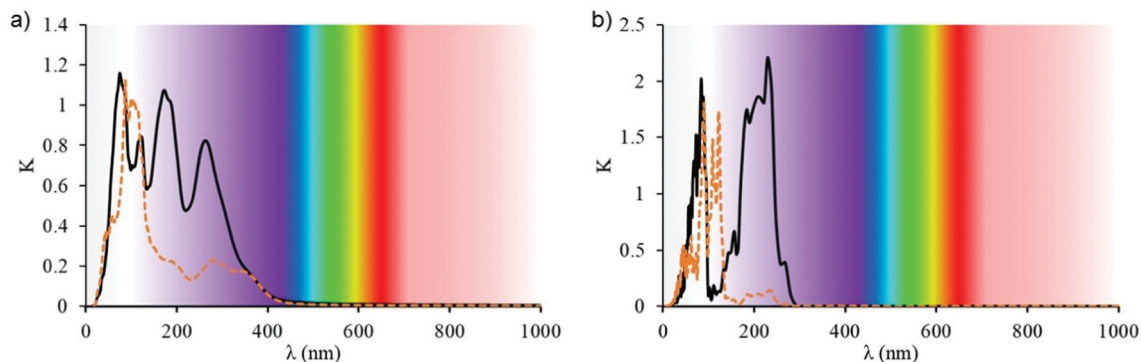


Fig. 4 Wavelength dependence of the extinction coefficient of (a) bulk  $B_5N_3O_2$  and (b) bulk h-BN. Black and orange lines correspond to the longitudinal and transverse directions, respectively.

linear dependence:  $C_{11} = \frac{\sigma_1}{\eta_1}$ ;  $C_{22} = \frac{\sigma_2}{\eta_2}$ ;  $C_{12} = \frac{\sigma_1}{\eta_2}$ . The 2D linear elastic constants calculated for  $B_5N_3O_2$  ( $C_{11} = 201.8 \text{ N m}^{-1}$ ,  $C_{22} = 75.7 \text{ N m}^{-1}$ , and  $C_{12} = 6.9 \text{ N m}^{-1}$ ) are lower than those of h-BN<sup>8–11</sup> and graphene<sup>8–10,12,13</sup> but higher than those of transition metal dichalcogenides<sup>11,14,15</sup> (Table 1). The estimated values of the 2D elastic constants of the other B–N–O structures considered in this study are presented in Fig. S7 (ESI†). The new B–N–O nanostructures have more defective and less dense structure, and therefore lower elastic constants, than those with the oxygen concentrations of 20 and 10 atom % studied previously.<sup>7</sup> However, the B–N–O compositions described by Singh *et al.*<sup>42</sup> have a hexagonal h-BN structure with oxygen substituting some nitrogen atoms. The calculated elastic constant  $C_{11}$  of  $B_5N_3O_2$  is comparable with that of the B–N–O composition with 20 atom % of oxygen and at the same time is higher than those of the monolayers of transition metal dichalcogenides  $MoS_2$  and  $WS_2$ . Moreover, drastic changes in the atomic structure caused by the presence of oxygen may influence the electric response of B–N–O compositions under external mechanical deformation. The irregular geometry of  $B_5N_3O_2$  may lead to a nonzero local dipole moment, which could play a significant role in the emergence or enhancement of piezoelectricity. We carried out *ab initio* calculations of the local dipole moments of the 5-member rings of  $B_5N_3O_2$  and a part of the 6-member ring with oxygen (red and blue rectangles in Fig. S6, ESI†). Uncompensated local dipole moments of 6.21 D and 11.5 D were found in the 5- and 6-member rings, respectively. The directions of these local dipole moments are  $\vec{n} = (0.54; 0.77; -0.32)$  and  $\vec{n} = (0.04; 0.94; 0.31)$ , respectively. The presence of nonzero local dipole moments of the individual components may indicate prospects for applications in the field of piezoelectric materials and requires a separate study. The 2D piezoelectric tensor of the B–N–O structures was also estimated (Table S1, ESI†).

### Optical properties

Using the wavelength dependences of permittivity components, by means of the PBE functional<sup>27</sup> we estimated the extinction coefficient of  $B_5N_3O_2$ , which shows the capability to absorb electromagnetic radiation at different wavelengths. For

polarized light propagating in both transverse and longitudinal directions to the oxynitride layers, the absorption peaks of  $B_5N_3O_2$  are shifted closer to the visible range but are still located in the ultraviolet area (Fig. 4a) in comparison with pure h-BN (Fig. 4b). In the ultraviolet region with  $\lambda = 200\text{--}400 \text{ nm}$ , the absorption of the longitudinally propagating radiation is significantly higher than that of the perpendicularly propagating radiation. We also carried out the calculations of dependence of the extinction coefficient on the wavelength by applying the HSE06 hybrid functional<sup>53</sup> (see Fig. S6 in the ESI†). The obtained data states about the larger absorption in the ultraviolet region with  $\lambda = 200\text{--}400 \text{ nm}$  in comparison with h-BN.

## IV. Conclusions

Using the USPEX evolutionary algorithm, we predicted the structures of the  $B_xN_yO_z$  two-dimensional nanoscale arrangements. Along with compositions in which some nitrogen atoms are replaced by oxygen, unique B–N–O structures were found. The experimental data on the synthesis of boron oxynitride suggests a larger interplanar distance than in pure h-BN. Among the structures we predicted,  $B_5N_3O_2$  has the oxygen concentration similar to that of an experimentally obtained composition and a similarly expanded interplanar distance. This may indicate that its structure is probably different from the hexagonal arrangement of h-BN with incorporated oxygen atoms that can be observed experimentally. The elastic constants of the predicted compositions are comparable with the mechanical properties of boron nitride. We assumed that the incorporation of oxygen atoms into the structure of 2D BN can cause local dipole moments which might improve its piezoelectric properties. The calculated electronic structure shows a decrease in the bandgap caused by the addition of oxygen, which also leads to a red shift of absorption peaks toward near UV region. Our results explain the puzzling properties of oxidized BN sheets determined in previous experiments.

## Conflicts of interest

There are no conflicts to declare.

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