



# Electrides: in pursuit of correlations

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November 12

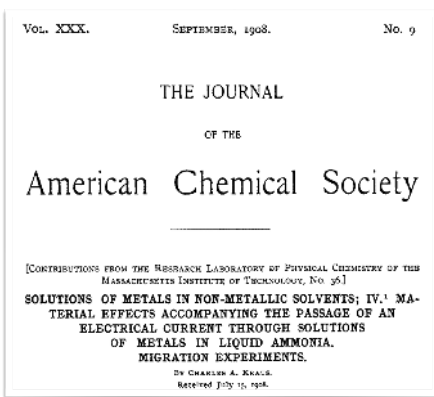
19th ONLINE USPEX workshop  
Moscow, Russia



Supported by the Russian Scientific Foundation grant No. 19072-30043 "Computational materials design laboratory"

What color is an electron?

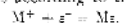
- Blue
- Green
- Yellow



The negative ion constitutes a new species of anion. It consists of a negative charge, an electron, surrounded by an envelope of solvent molecules. The electron is thus in equilibrium with ammonia according to the equation:



At the same time the electron is in equilibrium with the metal cations and the neutral metal atoms according to the equation

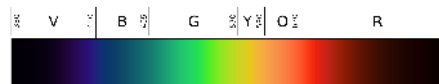


where  $\text{M}^+$  signifies the cation and  $\text{M}_0$  the neutral atom.

BOSTON, July 14, 1908.

## Independent electrons

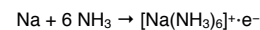
The absorption band of a solvated electron:  
 in water and ammonia 720 nm  
 in methanol 625 nm  
 in ethanol 680 nm  
 in decanol 650 nm



Lithium solution in liquid ammonia:

- the dark blue color corresponds to the insulating state
- golden (concentration more than 3 moles) - conductor

**Sodium dissolves in liquid ammonia ( $\text{NH}_3$ )**

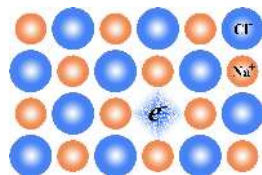


Cotton, F. A.; Wilkinson, G. (1972). *Advanced Inorganic Chemistry*. John Wiley and Sons Inc. ISBN 978-0-471-17560-5.

Schindewolf, U. (1968). "Formation and Properties of Solvated Electrons". 7 (3): 190-203. doi:10.1002/anie.196801901.  
 Cotton, F. A.; Wilkinson, G. (1972). *Advanced Inorganic Chemistry*. John Wiley and Sons Inc. ISBN 978-0-471-17560-5.

### Halite (NaCl)

(derived from the Ancient Greek word for salt, ἅλς (hals))



### First crystalline electride Cs\*(18-Crown-6)<sub>2</sub>e<sup>-</sup>

*J. Am. Chem. Soc.* **1983**, *105*, 6490-6491

*J. Am. Chem. Soc.* **1986**, *108*, 3534-3535

#### Cesium 18-Crown-6 Compounds. A Crystalline Cesium and a Crystalline Electride

Ahmed Ellaboudy and James L. Dye\*

Department of Chemistry, Michigan State University  
East Lansing, Michigan 48824

Patrick B. Smith

Dow Chemical Company

Midland, Michigan 48640

Received July 22, 1983

#### First Electride Crystal Structure

Steven B. Dawes, Donald L. Ward, Rui He Huang, and James L. Dye\*

Department of Chemistry, Michigan State University  
East Lansing, Michigan 48824

Received January 21, 1986

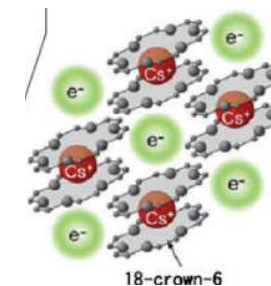
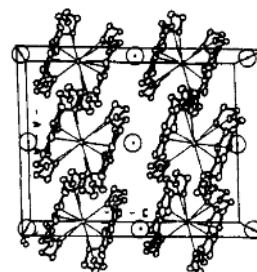
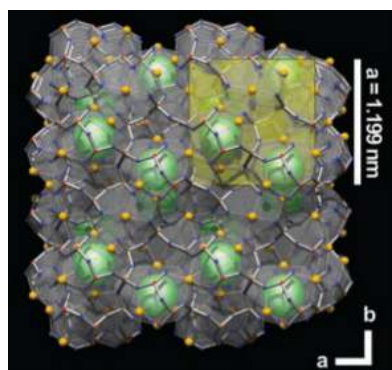


Figure 1. ORTEP stereo packing diagram of Cs\*(18C6)<sub>2</sub>e<sup>-</sup>. The anionic hole centers are indicated by the symbol ⊖.

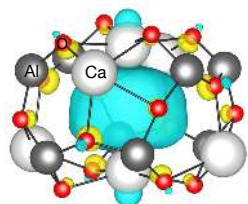
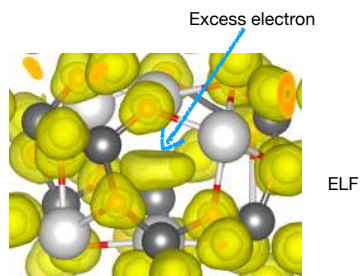
### First inorganic electride [Ca<sub>24</sub>Al<sub>28</sub>O<sub>64</sub>]<sup>4+</sup>4e<sup>-</sup>

$I\bar{4}3d$



Matsuishi S, Toda Y, Miyakawa M, Hayashi K, Kamiya T, Hirano M, Tanaka I, Hosono H. *Science* **301**, 626-629 (2003)

$$n_e \sim 2.33 \cdot 10^{21} \text{cm}^{-3}$$



Spatial distribution of the MLWF describing the electride state.

### Applications

#### \* Electron emitters

Huang, R. H. & Dye, J. L. Low temperature (-80°C) thermionic electron emission from alkaliides and electrides. *Chem. Phys. Lett.* **166**, 133-136 (1990).

#### \* Superconductors (room temperature!)

Hosono, H. et al. Superconductivity in room-temperature stable electride and high-pressure phases of alkali metals. *Philos. Trans. R. Soc. A Math. Phys. Eng. Sci.* **373**, (2015).

#### \* Battery anodes

Hu, J. et al. 2D Electrides as Promising Anode Materials for Na-Ion Batteries from First-Principles Study. *ACS Appl. Mater. Interfaces* **7**, 24016-24022 (2015).

#### \* Optics (Ca<sub>2</sub>N as a natural hyperbolic metamaterial)

Guan, S., Huang, S. Y., Yao, Y. & Yang, S. A. Tunable hyperbolic dispersion and negative refraction in natural electride materials. *Phys. Rev. B* **95**, 1-6 (2017).

#### \* Cathode material in fluorescent lamps (mayenite)

Watanabe, S. et al. Secondary electron emission and glow discharge properties of 12CaO7Al<sub>2</sub>O<sub>3</sub> electride for fluorescent lamp applications. *Sci. Technol. Adv. Mater.* **12**, (2011).

#### \* Radioactive waste storage (mayenite encapsulates volatile fission products)

Kuganathan, N., Chronos, A. & Grimes, R. W. The encapsulation selectivity for anionic fission products imparted by an electride. *Sci. Rep.* **9**, 1-11 (2019).

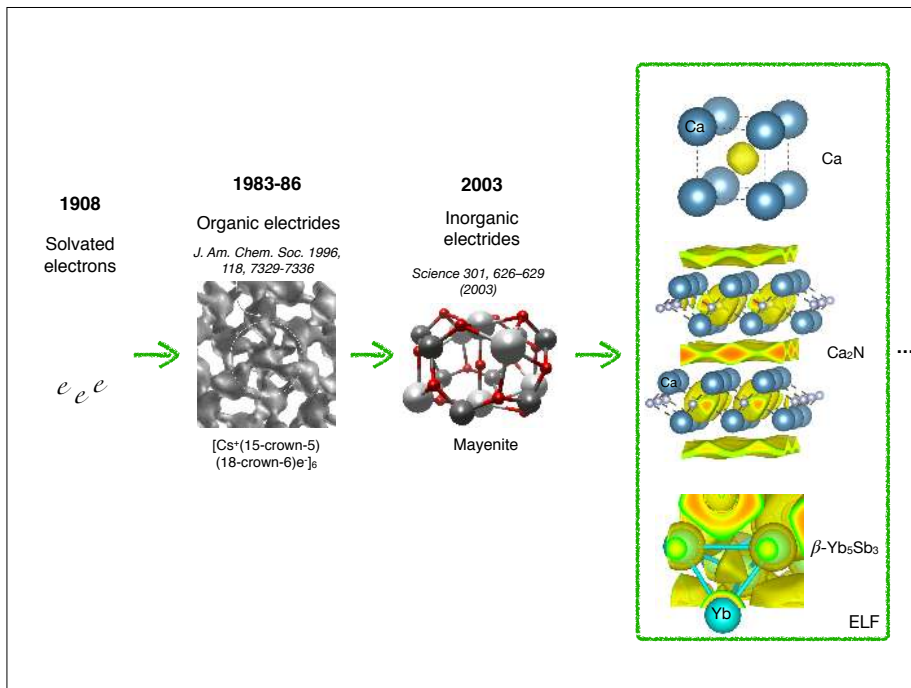
#### \* Catalysts for a range of applications

##### \* mayenite activate and split carbon dioxide at room temperature

Toda, Y. et al. Activation and splitting of carbon dioxide on the surface of an inorganic electride material. *Nat. Commun.* **4**, 1-8 (2013).

##### \* ammonia production

Kitano, M. et al. Ammonia synthesis using a stable electride as an electron donor and reversible hydrogen store. *Nat. Chem.* **4**, 934-940 (2012).



### Challenge

- Magnetic fluctuations (Ca<sub>2</sub>N, Yb<sub>5</sub>Sb<sub>3</sub>)
- Broadening and renormalisation of the electride bands (Ca<sub>2</sub>N)
- Lifetime of excited electride states (Yb<sub>5</sub>Sb<sub>3</sub>)
- Thermodynamically stable magnetic phase (Gd<sub>2</sub>C)
- Van der Waals interaction between layers that arises from the dipole-induced dipole interaction which is entirely due to correlation between electride electrons (2D-electrides)
- Structure transitions inaccessible in single-particle approximations (Ca, Ca<sub>2</sub>N)
- Insulator-metal transitions (Yb<sub>5</sub>Sb<sub>3</sub>)

What is the role of Coulomb correlations between anionic electrons in the formation of electride properties?

### Approach and tools

$\epsilon(\mathbf{k})$	DFT	<p><b>Quantum-ESPRESSO</b> Giannozzi, P. et al. <i>QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials.</i> <i>J. Phys. Condens. Matter</i> 21, 395502 (2009).</p> <p><b>VASP</b> Kresse, G. &amp; Furthmüller, J. <i>Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set.</i> <i>Phys. Rev. B</i> 54, 11169–11186 (1996).</p>
$H_{GGA}$	MLWF Wannier90	<p>Mostofi, A. A. et al. <i>An updated version of wannier90: A tool for obtaining maximally-localised Wannier functions.</i> <i>Comput. Phys. Commun.</i> 185, 2309–2310 (2014).</p>
$\Sigma, G$	DMFT AMULET CT-QMC Hybridization expansion	<p><a href="http://www.amulet-code.org">www.amulet-code.org</a></p> <p>Werner, P. &amp; Millis, A. J. <i>Hybridization expansion impurity solver: General formulation and application to Kondo lattice and two-orbital models.</i> <i>Phys. Rev. B</i> 74, 155107 (2006).</p>

### Structure transitions in elemental calcium

Li, B. et al. *Calcium with the β-tin structure at high pressure and low temperature.* *Proc. Natl. Acad. Sci. U.S.A.* 109, 16459–16462 (2012).

Oganov, A. R. et al. *Exotic behavior and crystal structures of calcium under pressure.* *Proc. Natl. Acad. Sci.* 107, 7646–7651 (2010).

Phase diagram of Ca at high pressure and low temperature.

**DFT method is not able to reproduce the transition to a simple cubic phase**

What is the nature of the stability of the SC structure at low temperatures?

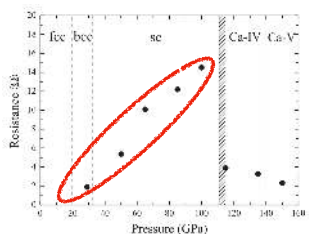
### Electride formation in Ca

Oganov, A. R. et al. Exotic behavior and crystal structures of calcium under pressure. Proc. Natl. Acad. Sci. 107, 7646–7651 (2010).

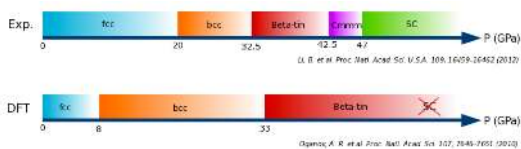


Valence ELF (including semicore 3s and 3p-states) of fcc-Ca at 1 atm and 18 GPa.

«ELF has maxima not only at the nuclei, but also in the octahedral voids between them. These maxima become much more pronounced on increasing pressure»

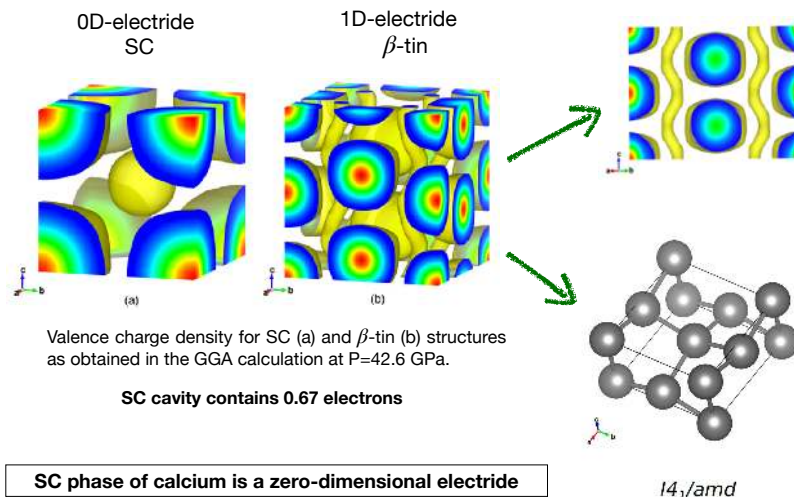


Yabuuchi, T. et al., J. Phys. Soc. Japan 74, 2391 (2005).



Could the electride states and correlations be responsible for SC structure stability?

### Charge density of Ca under pressure



Valence charge density for SC (a) and  $\beta$ -tin (b) structures as obtained in the GGA calculation at P=42.6 GPa.

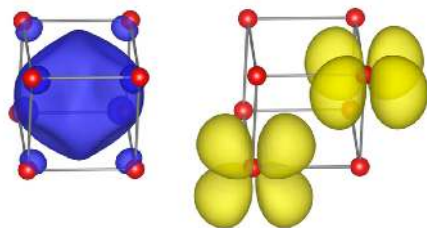
SC cavity contains 0.67 electrons

SC phase of calcium is a zero-dimensional electride

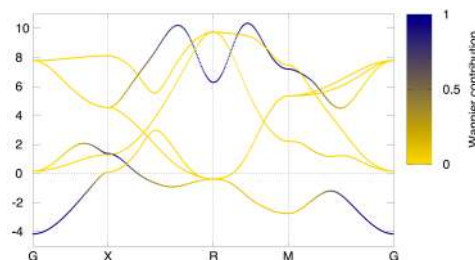
$14_1/amd$

### Interstitial states in the bands of Ca

Wannier function of s-symmetry centered on the cubic void within the SC cell (left) and WFs of  $d_{xz}$ ,  $d_{xy}$ -symmetry (right). Ca atoms denoted with red spheres.



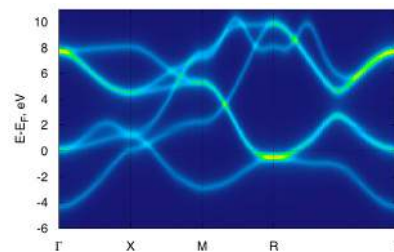
Band structure of SC Ca and contribution of the WF with s-symmetry centered on interstice to the Bloch states.



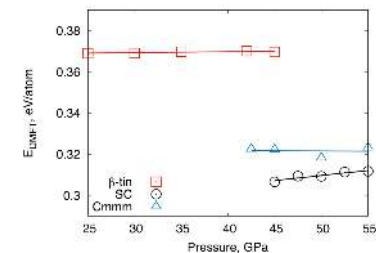
### Coulomb parameter U and DMFT correlation energy in Ca

The constrained DFT procedure: U=0.47eV

Anisimov, V. I. & Gunnarsson, O. Density-functional calculation of effective Coulomb interactions in metals. Phys. Rev. B 43, 7570–7574 (1991).



ARPES for the SC structure obtained in the DFT+DMFT calculation for  $V=18.23 \text{ \AA}^3$ .

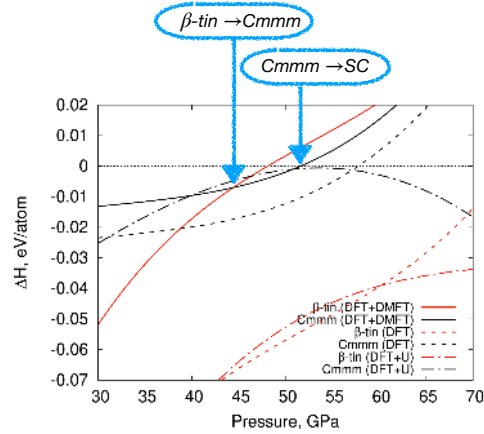


DMFT energy correction.

The total energy correction due to the correlation effects almost does not depend on applied pressure for the considered structures.



### Correlations and phase transitions in Ca

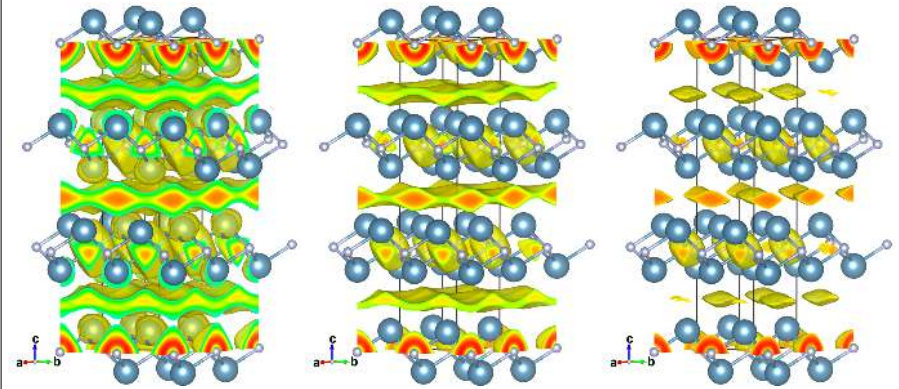


Enthalpy of beta-tin (red) and Cmmm (black) phases of Ca under pressure obtained in the DFT (dashed lines) and DFT+DMFT (solid lines) with respect to SC shown by zero line.

**Correlation effects are strong enough to result in the correct phase sequence in Ca under pressure.**

Novoselov, D. Y., Korotin, D. M., Shorikov, A. O., Oganov, A. R. & Anisimov, V. I. Weak Coulomb correlations stabilize the electride high-pressure phase of elemental calcium. *J. Phys. Condens. Matter* 32, 445501 (2020).

### First 2D electride [Ca<sub>2</sub>N]<sup>+e-</sup>



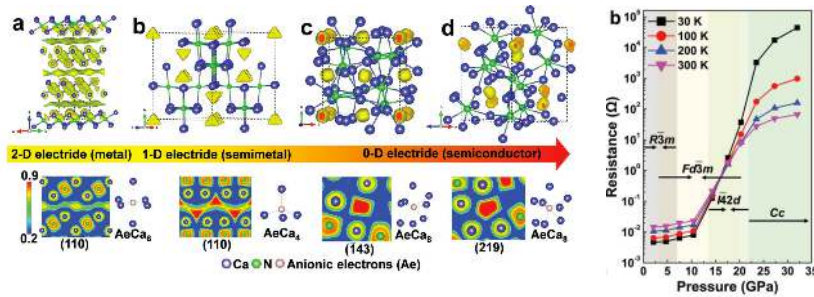
ELF=0.25

ELF=0.5

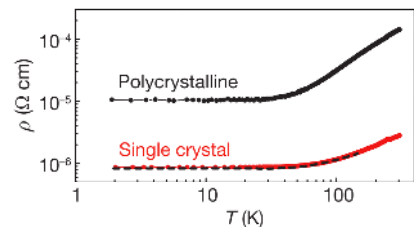
ELF=0.65

Excess electrons are in a quasi-two-dimensional region between Ca<sup>2+</sup> ions located in the outermost positions of each layer, which provides electrostatic stability for electrons.

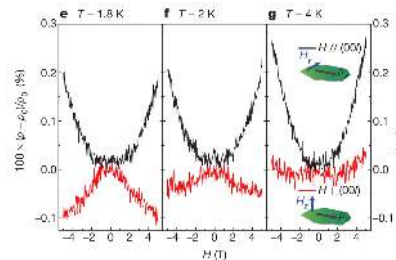
### First 2D electride [Ca<sub>2</sub>N]<sup>+e-</sup>



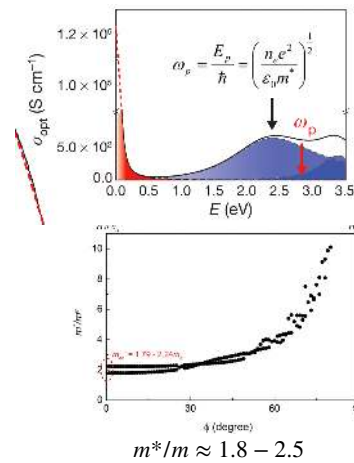
Tang, H. et al. Metal-to-Semiconductor Transition and Electronic Dimensionality Reduction of Ca<sub>2</sub>N Electride under Pressure. *Adv. Sci.* 5, 2–7 (2018).



K. Lee, S. W. Kim, Y. Toda, S. Matsuishi and H. Hosono, *Nature*, 2013, 494, 336–340.

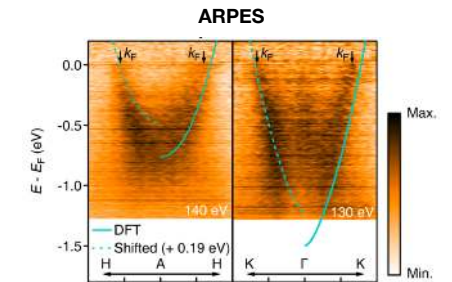


### Experimental evidence for anionic excess electrons in Ca<sub>2</sub>N and the theoretical challenges



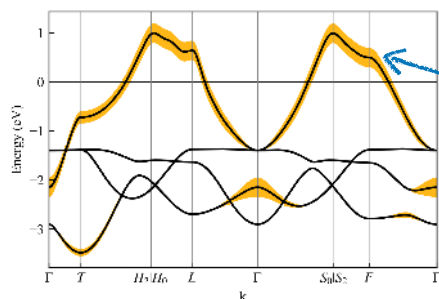
**How the Coulomb correlations affect the physical properties of Ca<sub>2</sub>N? How strong are the correlations?**

K. Lee, S. W. Kim, Y. Toda, S. Matsuishi and H. Hosono, *Nature*, 2013, 494, 336–340.

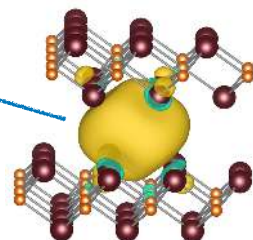


Oh, J. S. et al. *J. Am. Chem. Soc.* 138, 2496–2499 (2016).

### Interlayer states in Ca<sub>2</sub>N



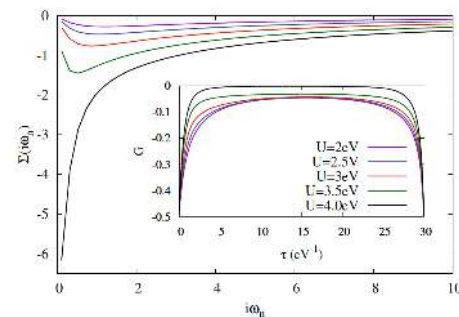
Band structure of Ca<sub>2</sub>N (black lines). The contribution to the Bloch states by the maximally localized Wannier function with s-symmetry centered on the electride layers is shown in yellow.



Spatial distribution of the MLWF describing the electride state. The Ca and N atoms are shown in reddish-purple and orange, respectively.

**The electrical conductivity of Ca<sub>2</sub>N is due to the electrons enclosed in the space between the layers.**

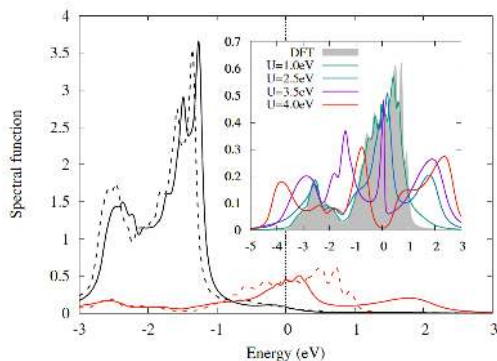
### Self-energy and Green's functions of electride states in Ca<sub>2</sub>N



Imaginary part of self-energy as a function of Matsubara frequencies at  $\beta=30 \text{ eV}^{-1}$  for different values of Coulomb parameter  $U$  and corresponding Green's functions in the inset.

**The value of Green function at half of beta indicates the metallic character of conductivity at intermediate values of  $U$ .**

### Spectral functions of Ca<sub>2</sub>N



Spectral functions obtained using DFT (dashed lines) and DFT+DMFT (solid lines) for  $\beta=30 \text{ eV}^{-1}$  and  $U=2.5 \text{ eV}$  resolved for the electride (red) and p-N (black) states. The spectral functions of the electride states obtained using DFT and DMFT for different values of  $U$  are shown in the inset. Zero corresponds to the Fermi energy.

**An increase of  $U$  up to  $2.5 \text{ eV}$  leads to a renormalization of the spectral weight and narrowing of the band around the Fermi level.**

### Electron mass enhancement and $U$ in Ca<sub>2</sub>N

$$m^*/m = 1 - \left. \frac{\partial \Sigma}{\partial \omega} \right|_{\omega=0}$$

TABLE I. Effective electron mass enhancement  $m^*/m$  and the Fermi level shift relative to DFT value obtained using DMFT at  $\beta = 30 \text{ eV}^{-1}$ . The experimentally determined electron mass enhancement is 1.9-2.5 [7].

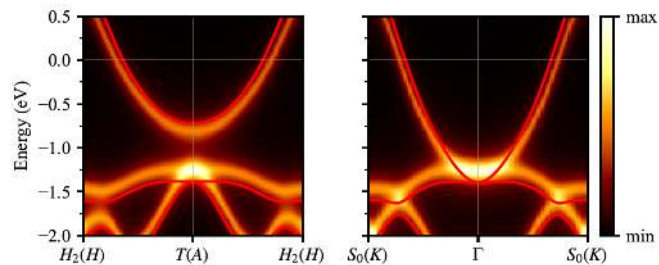
	$U=2 \text{ eV}$	$U=2.5 \text{ eV}$	$U=3 \text{ eV}$	$U=3.5 \text{ eV}$
$m^*/m$	1.74	2.35	3.62	9.21
$\Delta E_F$	0.07	0.09	0.12	0.16

Linear response:  $U=2.78 \text{ eV}$

**At  $U=2.5 \text{ eV}$ , the  $m^*/m$  equals  $2.35m_e$ , which agrees better with the experimental value of  $1.9\text{--}2.5m_e$  and the paramagnetic solution with a local instant squared magnetic moment of  $0.76\mu_B$  per electride site.**

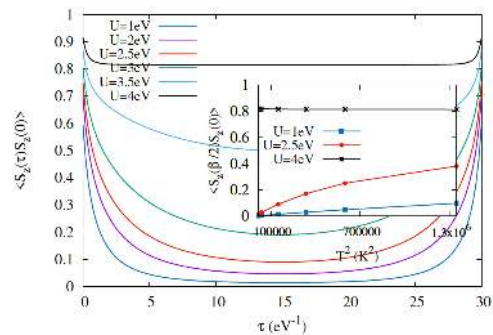
### ARPES of Ca<sub>2</sub>N

ARPES obtained in DMFT calculations at  $\beta=60$  eV<sup>-1</sup> with  $U=2.5$  eV. Band structure from DFT calculations is shown by solid red lines.



Dynamic Coulomb correlations between the confined electrons lead to the shift of the Fermi level and renormalization of the bands, as well as to their smearing.

### Magnetic properties of Ca<sub>2</sub>N

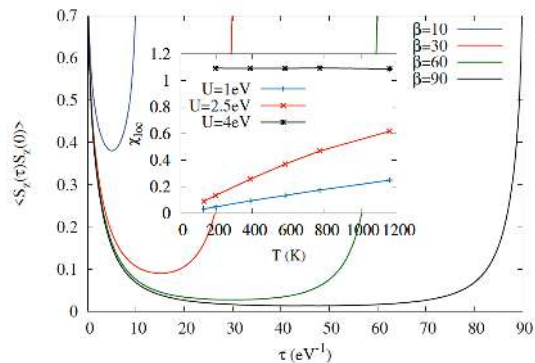


Local spin-spin correlation functions in the imaginary-time domain obtained using DFT+DMFT at  $\beta=30$  eV<sup>-1</sup> for different values of the Coulomb parameter  $U$ . Inset: Dependence of the spin-spin correlation function on  $T^2$  at  $\tau=\beta/2$  and  $U=1, 2.5,$  and  $4$  eV.

$$U = 4\text{eV} : \langle S_z(\tau)S_z(0) \rangle \approx S^2$$

For  $U=2.5$  eV, the curve of  $\langle S_z(\beta/2)S_z(0) \rangle$  lies between those for  $U=1$  and  $4$  eV, which indicates an intermediate regime with partially localized electrons that is closer to the Fermi liquid at high temperatures.

### Local spin susceptibility of Ca<sub>2</sub>N



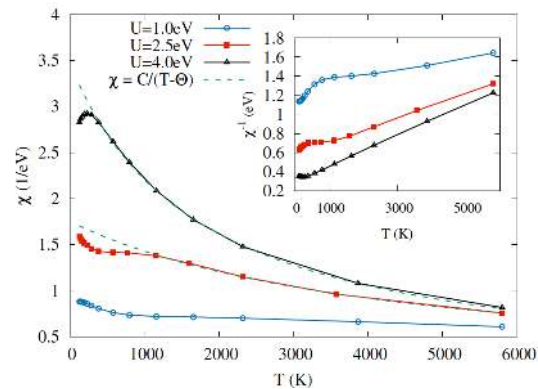
$$\chi_{\text{loc}} = g_s^2/3 \cdot \int_0^\beta d\tau \langle \mathbf{S}(0)\mathbf{S}(\tau) \rangle$$

$$g_s = 2$$

Local spin-spin correlation functions in the imaginary-time domain obtained using DFT+DMFT at  $U=2.5$  eV for different values of  $\beta$ . Inset: Temperature dependence of the local spin susceptibility at  $U=1, 2.5,$  and  $4$  eV.

Partially localized and relatively large magnetic moments are present in the interstitial sites for  $U=2.5$  eV.

### Magnetic susceptibility of Ca<sub>2</sub>N



$$\chi(T) = m(T)/H_z$$

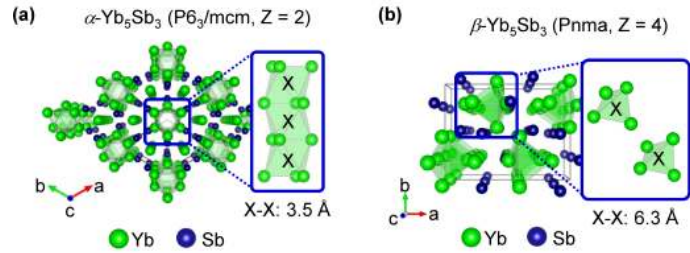
$$m(T) = \sum_m (n_m^\uparrow - n_m^\downarrow)$$

Temperature dependencies of the uniform magnetic susceptibility and its inverse (in the inset).

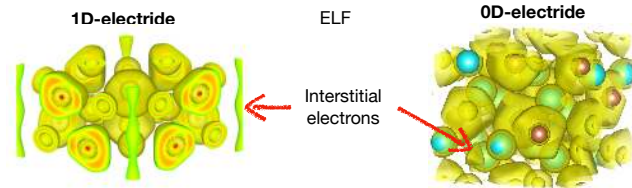
The Stoner-type ferromagnetic instability prevails at low temperatures, and an increase in the temperature leads to a growth in the localization of the moments and a strengthening of the antiferromagnetic interaction.



### Dimorphic $[\text{Yb}_5\text{Sb}_3]^{+e^-}$

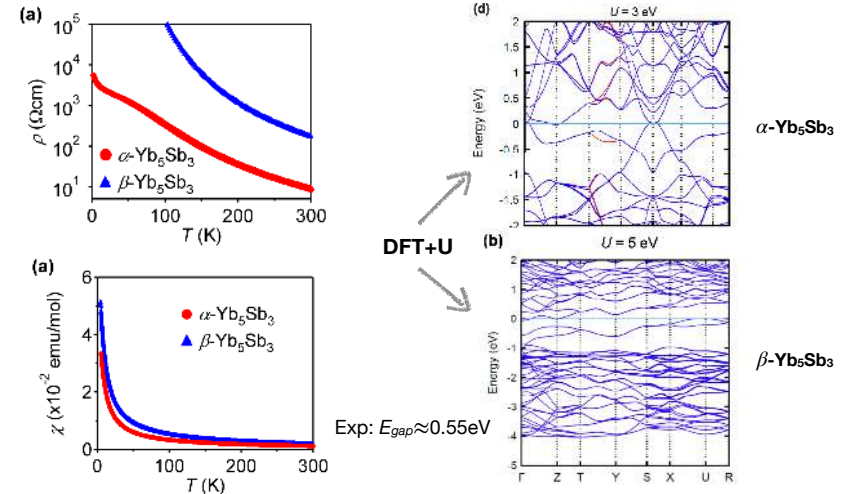


Yangfan Lu, Junjie Wang, Jiang Li, Jiazhen Wu, Shu Kanno, Tomofumi Tada and Hideo Hosono PRB 98, 125128 (2018).



The smaller dimension of the cavities leads to a more pronounced localization of the electride states.

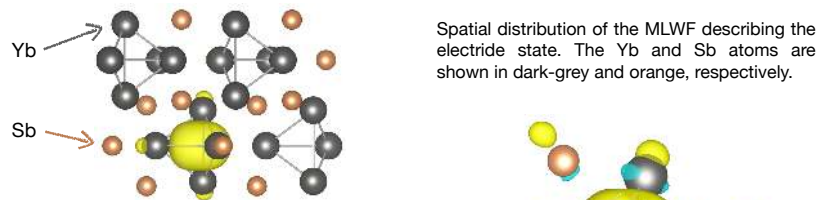
### Exp. and DFT+U



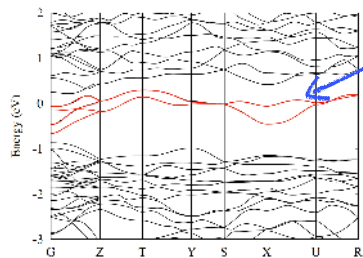
Yangfan Lu, Junjie Wang, Jiang Li, Jiazhen Wu, Shu Kanno, Tomofumi Tada and Hideo Hosono PRB 98, 125128 (2018).

What is the role of electride states in semiconductor behavior and magnetism in  $\beta\text{-Yb}_5\text{Sb}_3$ ?

### Interstitial electronic states of $\beta\text{-Yb}_5\text{Sb}_3$

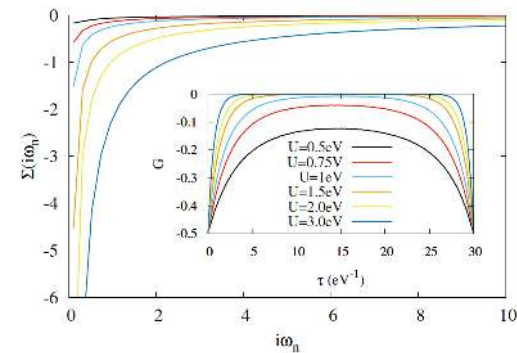


Crystal structure of  $\beta\text{-Yb}_5\text{Sb}_3$  with isosurface of one MLWF localized in the tetrahedral cavity.



DFT band structure of  $\beta\text{-Yb}_5\text{Sb}_3$  (black lines). Fermi level corresponds to zero.

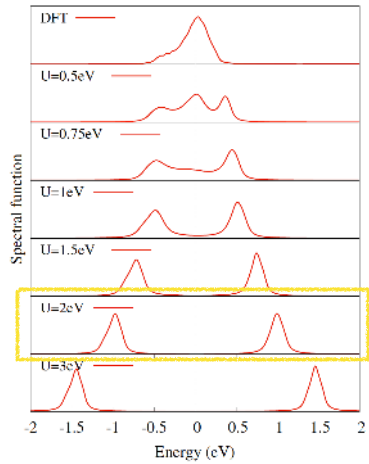
### Metal-insulator Mott transition in $\beta\text{-Yb}_5\text{Sb}_3$



$G(\beta/2)$  indicates the evolution from metallic to the insulating character of conductivity with the growth of  $U$ .



### Metal-insulator Mott transition in $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub>



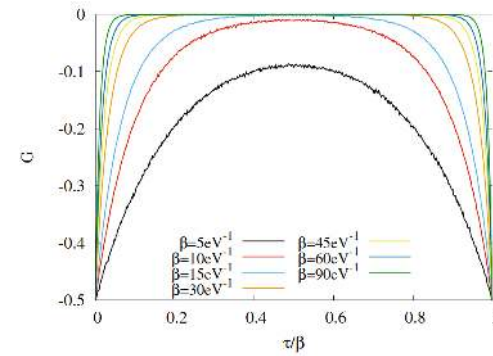
The Mott insulator state in  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> electrider exists due to the Coulomb interactions of the electrons not related to specific sites of the crystal lattice

Exp:  $E_{gap} \approx 0.55 \text{ eV}$

Yangfan Lu, Junjie Wang, Jiang Li, Jiazhen Wu, Shu Kanno, Tomofumi Tada and Hideo Hosono PRB 98, 125128 (2018).

Spectral functions obtained using DFT (top panel) and DFT+DMFT for different values of U at  $\beta=30 \text{ eV}^{-1}$ . Zero corresponds to the Fermi energy.

### Semiconducting behavior of $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub>

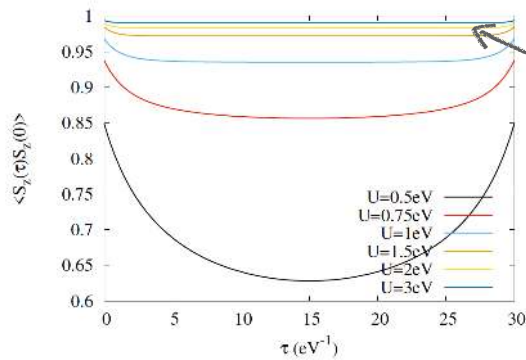


Temperature decreases  
 $T = \frac{1}{k_B \beta}$

Green's functions at  $U=2 \text{ eV}$  and different values of the  $\beta$  parameter

The semiconducting behavior of  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> is caused by Coulomb correlations between the electrider electrons

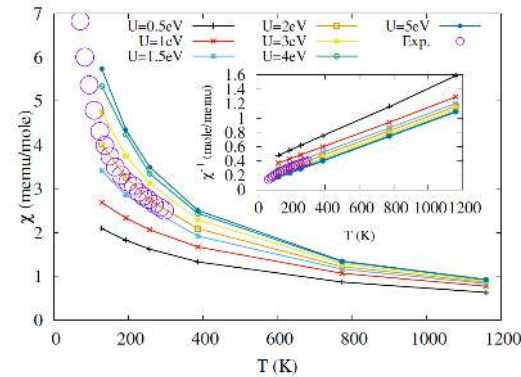
### Localization and magnetism in $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub>



At the value of  $U=2 \text{ eV}$  each the electrider density acts as the magnetic center with  $S=1/2$ .

Local spin-spin correlation functions  $\langle S_z(\tau)S_z(0) \rangle$  in the imaginary-time domain obtained using DFT+DMFT at  $\beta=30 \text{ eV}^{-1}$  for different values of the Coulomb parameter U

### Localization and magnetism in $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub>



$$\chi(T) = m(T)/H_z$$

$$m(T) = \sum_m (n_m^{\uparrow} - n_m^{\downarrow})$$

The model mainly derived from the interstitial anionic electronic states properly describes the magnetic features of  $\beta$ -Yb<sub>5</sub>Sb<sub>3</sub> with the moderate value of the Coulomb parameter U.

Temperature dependencies of the uniform magnetic susceptibility  $\chi(T)$  and its inverse (in the inset) for different values of U as well as the experimental data [1] shown by the violet circles.

### **Conclusion remarks**

- Electride states can be correlated while the strength of correlations can vary from weak to strong.
- Coulomb correlations between electrons described by electride states can directly be related to the most interesting physical properties of such materials including structural transitions, metal-insulator transitions, strong interstitial local magnetic moments and magnetic fluctuations.
- Properly describing the electride states and taking into account dynamical correlation effects make it possible to correctly model both already known electrifies and to search for and predict new ones.

Thank you for your attention!